

# An Insulin Infusion Advisory System Based on Autotuning Nonlinear Model-Predictive Control

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**Abstract**—This paper aims at the development and evaluation of a personalized insulin infusion advisory system (IIAS), able to provide real-time estimations of the appropriate insulin infusion rate for type 1 diabetes mellitus (T1DM) patients using continuous glucose monitors and insulin pumps. The system is based on a nonlinear model-predictive controller (NMPC) that uses a personalized glucose–insulin metabolism model, consisting of two compartmental models and a recurrent neural network. The model takes as input patient’s information regarding meal intake, glucose measurements, and insulin infusion rates, and provides glucose predictions. The predictions are fed to the NMPC, in order for the latter to estimate the optimum insulin infusion rates. An algorithm based on fuzzy logic has been developed for the on-line adaptation of the NMPC control parameters. The IIAS has been *in silico* evaluated using an appropriate simulation environment (UVa T1DM simulator). The IIAS was able to handle various meal profiles, fasting conditions, interpatient variability, intraday variation in physiological parameters, and errors in meal amount estimations.

**Index Terms**—Artificial pancreas (AP), autotuning model-predictive control, personalized model, type I diabetes mellitus (T1DM).

## I. INTRODUCTION

INSULIN-dependent diabetes mellitus is a metabolic disorder, characterized by the disability of the body to regulate blood glucose (BG) levels. Particularly, it is an autoimmune disease in which the  $\beta$ -cells of the pancreas are destroyed, resulting in the absence of insulin secretion. Chronic elevation

of BG level leads to damage of blood vessels (angiopathy), resulting in serious long-term complications, such as blindness, neuropathy, heart disease, and kidney failure. According to the diabetes control and complications trial [1], the aforementioned complications can be reduced by intensive glycemic control, which involves regular glucose measurements and exogenous insulin administration. Latest advances in technology have led to the development of continuous glucose monitors (CGMs) that provide subcutaneous (sc) glucose measurements at a high frequency [2], and insulin pumps for continuous sc insulin infusion.

The experience with CGMs and insulin pumps, along with advances in computational algorithms for the automatic estimation and adjustment of appropriate insulin infusion rates makes the development of a wearable artificial pancreas (AP) feasible [3]. Closed-loop glucose control systems can be categorized according to the way mealtime insulin delivery is handled. In “fully closed-loop” mode, insulin is delivered without information about the time or size of the meal. In “semiclosed-loop” control, the controller is provided with information regarding the meal size and generates advice on prandial insulin. A significant benefit to controller performance can be obtained, when meal information is provided. Although a wide range of algorithms have been proposed [4], the most common approaches are based on proportional integral derivative controller [5], [6], and model-predictive controller (MPC) [7]–[16]. MPC (linear and nonlinear) seems to be the most appropriate for the development of AP, since it is able to handle problems related to 1) high nonlinearity of the glucose–insulin metabolism, caused by saturation and inhibition effects evidenced by chemical substrates and hormones involved in enzyme dynamics and hormonal control effects, 2) time delays in sc–sc route due to the delayed effect of infused sc insulin and food intake to the blood and, consequently, of glucose diffusion from the blood to the sc space, and the lag time between sc glucose value and glucose sensor (in the case of sensors based on microdialysis or microperfusion), and 3) noise to the sc glucose measurements. The models used to develop glucose controllers based on linear MPC are usually discrete linearized state-space models obtained from the average original nonlinear patient’s model, which serves as the *in silico* T1DM patient for the evaluation of the glucose controllers [7], [8], [12]. However, such an approach would suffer from the lack of personalization [4] and from dependencies between the predictive model integrated in the glucose controller and the *in silico* patient model, thus limiting the reliability of the *in silico* evaluation of the controller. A model-predictive iterative learning control has been proposed based on

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80 a data-driven linear autoregressive exogenous model (ARX) [9].  
 81 Although this model cannot describe accurately the real relation-  
 82 ship between glucose and insulin in T1DM, the proposed  
 83 control law performed well, especially in the case of repetitive  
 84 diets. Meal detection and meal size estimation algorithms have  
 85 been developed to improve meal glucose disturbance rejection  
 86 when incoming meals are not announced [11]. Furthermore,  
 87 several attempts have been made toward the development of  
 88 glucose controllers based on nonlinear model-predictive control  
 89 (NMPC), [10], [13] [14] and the effectiveness of the NMPC over  
 90 the linear MPC has been studied [14]. The models used to de-  
 91 velop glucose controllers based on NMPC are usually derived by  
 92 compartmentalizing the various physiological components in-  
 93 volved in the human metabolic process [10], [14]. The fact that  
 94 some of the endocrine processes affecting glucose metabolism  
 95 are still not fully understood may limit the effectiveness of these  
 96 controllers. Moreover, experiments on real patients using NMPC  
 97 have been performed [14]–[16]. Clinical trials have been con-  
 98 ducted to investigate whether the closed-loop insulin delivery  
 99 could control overnight BG [17], [18].

100 A very important issue toward the implementation of MPC  
 101 is its tuning. Traditionally, the MPC has a set of tuning pa-  
 102 rameters, which add flexibility and influence its performance  
 103 and stability. Usually, their values are adjusted either via trial  
 104 and error procedures or by following general tuning guide-  
 105 lines [19]. Because of the overlapping effect of the MPC pa-  
 106 rameters, trial and error is a rather cumbersome task [20]. Fur-  
 107 thermore, systematic approaches following tuning guidelines  
 108 cannot be implemented online by control operators because the  
 109 glucose metabolism is subject to severe disturbances and chang-  
 110 ing operating conditions. In order to overcome the aforemen-  
 111 tioned problems, an on-line adaptive strategy for MPC based  
 112 on fuzzy logic has been proposed [20], which enables auto-  
 113 matic tuning of the parameters and results in good control  
 114 performance.

115 To account for the highly nonlinear nature of the gluco-regu-  
 116 latory system, this study aims at the design, development, and  
 117 evaluation of a novel Insulin Infusion Advisory System (IIAS)  
 118 based on NMPC, which makes use of a new personalized model  
 119 for the simulation of glucose–insulin metabolism in type 1 dia-  
 120 betes mellitus (T1DM). To address the day-to-day variability in  
 121 the glucose dynamics of a T1DM individual and the interpatient  
 122 variability, the proposed personalized approach incorporates a  
 123 data-driven model, able to capture the glucose metabolic behav-  
 124 ior taking into account patient specific information. Moreover,  
 125 an automatic algorithm for the adaptation of the NMPC’s control  
 126 parameters over time is introduced. The IIAS has been evalu-  
 127 ated using the UVa-type T1DM simulator [21], which has been  
 128 approved by the Food and Drug Administration as a substitute  
 129 for animals’ trial in preclinical testing of closed-loop AP control  
 130 algorithms.

## 131 II. METHODOLOGY

132 The proposed IIAS comprises two modules: 1) the person-  
 133 alized glucose–insulin metabolism model; and 2) the NMPC.  
 134 These modules along with the automatic algorithm for on-

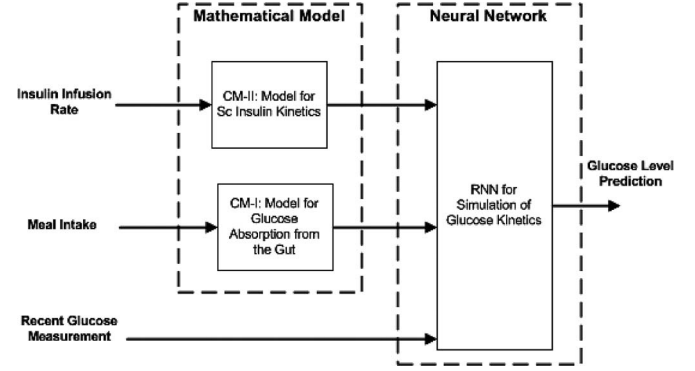


Fig. 1. Outline of the personalized glucose–insulin metabolism model used by the IIAS.

line tuning of NMPC control parameters are described in the following.

### A. Personalized Glucose–Insulin Metabolism Model

In order to provide the controller with glucose predictions ahead in time, a personalized glucose–insulin metabolism model (see Fig. 1) has been developed. The model is based on the combined use of a mathematical model (MM) module and a neural network (NN) module. The MM module consists of two Compartmental Models (CMs), which simulate sc insulin kinetics and glucose absorption into the blood from the gut, respectively, while the NN module incorporates a recurrent neural network (RNN), which models the patient’s glucose kinetics. Information regarding recent sc insulin infusion rate and meal intake are fed to the MM module. CMs’ outputs along with the recent sc glucose measurement are applied to the RNN that provides glucose predictions.

1) *CM for sc Insulin Kinetics*: Following an sc insulin injection, the rate of appearance of insulin in plasma [ $R_i(t)$ ] is described by a linear CM [22]:

$$\dot{I}_{sc1}(t) = -(k_d + k_{a1}) \cdot I_{sc1}(t) + u(t), \quad I_{sc1}(0) = I_{sc1ss} \quad (1)$$

$$\dot{I}_{sc2}(t) = k_d \cdot I_{sc1}(t) - k_{a2} \cdot I_{sc2}(t), \quad I_{sc2}(0) = I_{sc2ss} \quad (2)$$

$$R_i(t) = k_{a1} \cdot I_{sc1}(t) + k_{a2} \cdot I_{sc2}(t) \quad (3)$$

where  $I_{sc1}$  and  $I_{sc2}$  represent the amount of nonmonomeric and monomeric insulin in the sc space, respectively,  $u(t)$  (pmol/kg/min) is the exogenous insulin infusion rate,  $k_d$  (0.0164 min<sup>-1</sup>) is the rate constant of insulin dissociation, and  $k_{a1}$  (0.0018 min<sup>-1</sup>) and  $k_{a2}$  (0.0182 min<sup>-1</sup>) are the rate constants of nonmonomeric and monomeric insulin absorption, respectively.

2) *CM for Glucose Absorption From the Gut*: The physiological model of glucose intestinal absorption is a three-compartment nonlinear model with two compartments representing the stomach (solid and liquid phases) and the third compartment representing the intestine [22], [24]. The model assumes a constant rate of the intestinal absorption

167 but describes gastric emptying rate to be dependent on the  
168 total amount of nutrient in the stomach. Following a meal, the  
169 appearance rate of glucose in plasma,  $Ra$  (in mg/kg/min), is  
170 estimated by the following differential equations:

$$Q_{sto}(t) = Q_{sto1}(t) + Q_{sto2}(t), \quad Q_{sto}(0) = 0 \quad (4)$$

$$\dot{Q}_{sto1}(t) = -k_{gri} \cdot Q_{sto1}(t) + D \cdot d(t), \quad Q_{sto1}(0) = 0 \quad (5)$$

$$\dot{Q}_{sto2}(t) = -k_{empt}(Q_{sto}) \cdot Q_{sto2}(t) + k_{sto} \cdot Q_{sto1}(t),$$

$$Q_{sto2}(0) = 0 \quad (6)$$

$$\dot{Q}_{gut} = -k_{abs} \cdot Q_{gut}(t) + k_{empt}(Q_{sto}) \cdot Q_{sto2}(t),$$

$$Q_{gut}(0) = 0 \quad (7)$$

$$Ra(t) = \frac{f \cdot k_{abs} \cdot Q_{gut}(t)}{BW}, \quad Ra(0) = 0 \quad (8)$$

171 where  $Q_{sto}$  (in mg) is the amount of glucose in the stomach  
172 ( $Q_{sto1}$ , solid and  $Q_{sto2}$ , liquid phase),  $Q_{gut}$  (in mg) is the  
173 glucose mass in the intestine,  $k_{gri}(0.0558 \text{ min}^{-1})$  is the rate  
174 of grinding,  $k_{empt}(Q_{sto})$  ( $\text{min}^{-1}$ ) is the rate constant of gastric  
175 emptying, which is a nonlinear function of  $Q_{sto}$  [22], and  
176  $k_{abs}(0.057 \text{ min}^{-1})$  is the rate constant of intestinal absorption.  
177 Moreover,  $f(0.90)$ ,  $D$  (in mg) and  $BW$  (in kg) represent the  
178 fraction of intestinal absorption which appears in plasma, the  
179 amount of ingested glucose, and the body weight, respectively.

180 3) *RNN*: The use of the RNN toward the development of  
181 glucose–insulin metabolism model has been studied and its ability  
182 to accurately simulate glucose kinetics taking into account  
183 previous insulin and meal intakes, along with recent glucose  
184 levels, has been proven [25].

185 The RNN used in the proposed personalized glucose–insulin  
186 metabolism model is a fully connected multilayered perceptron  
187 NN with two recurrent loops, whose initial weights are set to  
188 unity [27], [28]. Subcutaneous glucose levels are considered  
189 as the state variable, while the rate of appearance of insulin in  
190 plasma and the glucose absorption into the blood from the gut  
191 as external inputs. Future glucose predictions are calculated as

$$y_{NN}(k+1) = y_{NN}(k) + RNN(y_{NN}(k), R_{\alpha}(k+1), R_i(k)) \quad (9)$$

192 where  $y_{NN}(k+1)$  and  $y_{NN}(k)$  are the sc glucose level predic-  
193 tions at instant  $k+1$  and  $k$ , respectively. The RNN is trained us-  
194 ing the Real-Time Recurrent Learning (RTRL) algorithm [29].  
195 RTRL is a sequential, error-correction learning-based algorithm,  
196 which allows the RNN to update the weights while operating.  
197 The teacher-force version of the RTRL [29] has been applied,  
198 according to which the RNN replaces the previous glucose level  
199 prediction with the corresponding glucose level value, when  
200 available, in order to produce future predictions. During the op-  
201 eration of the IIAS, the RNN's weights are updated based on  
202 the RTRL algorithm, whenever a new glucose measurement is  
203 applied. This effectively enables the adaptation of the glucose–  
204 insulin metabolism model to the special characteristics of the  
205 patient and to the diurnal variation of the glucose metabolism.  
206 Thus, the on-line training of the RNN ensures its stable perfor-  
207 mance for the entire input space.

## B. NMPC

208

209 As already mentioned, the NMPC uses a model that provides  
210 estimates of the future outputs of the system to be controlled. The  
211 NMPC is based on an optimizer, which computes at each sam-  
212 ple time future control movements based on the minimization  
213 of an appropriate cost function. Particularly, at each instant: 1)  
214 future outputs  $y_{NN}(k+i)$ ,  $i = N_1, \dots, N_p$  are generated by the  
215 prediction model; 2) a cost function of the future control move-  
216 ments is minimized providing a set of future control signals;  
217 and 3) only the first element of the suggested control sequence  
218 is applied to the system. The procedure is repeated at the next  
219 instant.

220 The definition of the cost function is critical to controller's  
221 performance. The cost function used in this paper [see (10)],  
222 consists of the standard MPC formulated cost function [30] and  
223 one penalty term [31]. Particularly, in (10), first and second  
224 terms represent the deviations of the glucose predictions from  
225 the reference glucose level  $r$ , and the changes in future insulin  
226 infusion rates, respectively, while the third term consists of two  
227 penalty terms, which add soft constraints ( $LG \leq y_{NN}(k+i) \leq$   
228  $HG$ ) to the optimization problem. The penalty terms increase  
229 the cost function whenever the glucose predictions are outside  
230 the acceptable range determined by the lowest ( $LG$ ) and the  
231 highest ( $HG$ ) desired glucose level. In (10),  $N_p$  is the prediction  
232 horizon,  $N_1$  is the minimum prediction horizon,  $N_c$  is the control  
233 horizon, and  $\Gamma_e$  and  $\Gamma_u$  are the prediction and control weighting  
234 coefficients, respectively, while  $\Gamma_L, \Gamma_H$  are penalty coefficients:

$$J = \Gamma_e \sum_{i=N_1}^{N_p} (y_{NN}(k+i) - r)^2 + \Gamma_u \sum_{j=0}^{N_c} \Delta u^2(k+j) \\ + \sum_{i=N_1}^{N_p} \left[ \Gamma_L [\min(0, y_{NN}(k+i) - LG)]^2 + \Gamma_H \sum_{j=1}^{N_c} \Delta u^2(k+j-1) \right. \\ \left. + \Gamma_H [\min(0, HG - y_{NN}(k+i))]^2 \right] \quad (10)$$

235 where

$$\Delta u(k) = u(k) - u(k-1). \quad (11)$$

236 The cost function is minimized, subject to the constraints

$$u_{\min} \leq u(k) \leq u_{\max}. \quad (12)$$

237 Regarding the values of the aforementioned parameters,  $N_p$  is  
238 usually chosen to encompass all the response, which is signifi-  
239 cantly affected by the current control signal (sc insulin infusion).  
240 If there is no evidence about the dead time,  $N_1 = 1$ . The choice  
241 of  $N_c$  is usually based on a compromise between good glucose  
242 control performance and minimization of on-line computation.  
243 Furthermore, the selection of  $r, LG, HG, \Gamma_L,$  and  $\Gamma_H$  is based  
244 on a compromise between ability to handle high glucose lev-  
245 els (caused by meal disturbances) and simultaneously prevent  
246 high values of insulin infusion rates, which would cause severe  
247 hypoglycaemic episodes.

248 In this paper, an automatic tuning algorithm, similar to the  
249 one proposed in [20], is adopted for the on-line update of the  
250 parameters  $N_p$  and  $\Gamma_u$ . These parameters play an important role

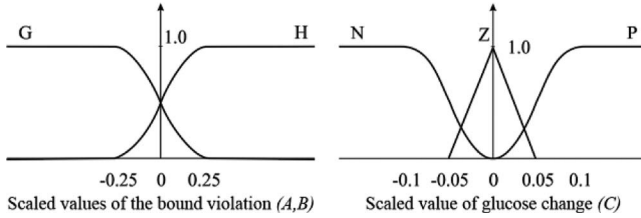


Fig. 2. Fuzzy sets for (a) bound violation and (b) bound violation rate.

251 to the controller's performance and stability. Although the time  
 252 to the peak action of sc insulin is considered to be 50 min, the  
 253 prediction horizon of 50 min is not always optimal, especially in  
 254 the presence of meal disturbances where glucose levels change  
 255 rapidly. This is of particular importance, since the sc glucose  
 256 measurements are subject to inaccuracies and there are lags  
 257 between the sc and the BG levels. The prediction weighting  
 258 coefficient  $\Gamma_e$  is chosen to be constant in order to avoid simul-  
 259 taneous increase of  $N_p$  and  $\Gamma_e$ , which would increase on-line  
 260 computation for the minimization of the cost function (10).

### 261 C. On-Line Tuning Algorithm of the NMPC Control Parameters

262 In order for the IIAS to rapidly reject meal disturbances  
 263 and maintain postprandial glucose levels within the acceptable  
 264 range, an automatic tuning algorithm has been developed. The  
 265 tuning technique adapts on-line the NMPC control parameters  
 266 in order to steer the closed-loop glucose response to satisfy pre-  
 267 set time-domain specifications, which are provided by the user  
 268 in the form of vectors of upper and lower bounds  $y^u$  and  $y^l$ ,  
 269 respectively. The new values of the NMPC control parameters  
 270 are determined by fuzzy logic rules.

271 1) *Overview of the Adaptation Algorithm:* The proposed  
 272 tuning method consists of two phases: the observation phase  
 273 and the triggered phase. In the former, the future glucose profile  
 274 is predicted, through the minimization of (10), by applying fixed  
 275 values to the prediction horizon  $P_w$  and the control weighting  
 276 coefficient  $\Gamma_{uw}$ . The obtained glucose profile is checked against  
 277 the performance envelope. In case a bound violation occurs, the  
 278 algorithm enters the triggered phase, otherwise the calculated  
 279 insulin infusion rate is applied to the system and the whole pro-  
 280 cedure is repeated at the next instant. Particularly, at each instant  
 281  $k$ , the steps of the tuning algorithm are as follows.

282 *Step 1.* Produce future glucose profile using fixed NMPC  
 283 control parameters through the minimization of the cost function  
 284 (10). The calculated insulin infusion rate at this step is not  
 285 applied to the patient.

286 *Step 2.* Check whether the predicted glucose profile, exceeds  
 287 the limits of the performance envelope, i.e.,  $y^u$  and  $y^l$ . If the  
 288 limits are not exceeded, go to step 8.

289 *Step 3.* Determine the corresponding glucose prediction and  
 290 the instant at which maximum bound violation occurs. Let this  
 291 be at instant  $k + m$ .

292 *Step 4.* Calculate the scaled values of the bound violation  
 293 ( $A, B$ ), and the glucose change ( $C$ ) at instant  $k + m$ .

294 *Step 5.* Determine the degree of membership of  $A, B$ , and  $C$   
 295 with respect to membership functions presented in Fig. 2.

TABLE I  
BASE RULES OF THE TUNING ALGORITHM

No.	Rule	Result of $\Gamma_u$	Result of $N_p$
R1	If $A$ is H and $B$ is G	Then $\mu_r$ is SN	Then $\mu_{Np}$ is LP
R2	If $A$ is G and $B$ is H	Then $\mu_r$ is LN	Then $\mu_{Np}$ is LP
R3	If $A$ is G and $B$ is G	Then $\mu_r$ is ZE	Then $\mu_{Np}$ is SN
R4	If $A$ is H and $C$ is P	Then $\mu_r$ is LN	Then $\mu_{Np}$ is SP
R5	If $A$ is H and $C$ is Z	Then $\mu_r$ is SP	Then $\mu_{Np}$ is SN
R6	If $A$ is H and $C$ is N	Then $\mu_r$ is ZE	Then $\mu_{Np}$ is ZE
R7	If $B$ is H and $C$ is P	Then $\mu_r$ is SN	Then $\mu_{Np}$ is ZE
R8	If $B$ is H and $C$ is Z	Then $\mu_r$ is SP	Then $\mu_{Np}$ is SN
R9	If $B$ is H and $C$ is N	Then $\mu_r$ is ZE	Then $\mu_{Np}$ is SP

296 *Step 6.* Calculate the correction factors  $[w_k(N_p), w_k(\Gamma_u)]$ .

297 *Step 7.* Set the new parameters values as

298  $N_{p,k} = N_{p,previous} + w_k(N_p)$  and  $\Gamma_{u,k} = \Gamma_{u,previous}$   
 299  $(1 + w_k(\Gamma_u))$ , where  $N_{p,previous}$  and  $\Gamma_{u,previous}$  are calculated  
 300 during the previous triggered phase of the tuning algorithm.

301 *Step 8.* Compute and apply the sc insulin infusion rate. Pro-  
 302 ceed to the next instant  $k + 1$  and go to step 1.

303 The initial values of  $N_p$  and  $\Gamma_u$  are set to  $P_w$  and  $\Gamma_{uw}$ , re-  
 304 spectively. In the presence of a meal disturbance, the control  
 305 parameters are appropriately updated in order to reduce the  
 306 overshoot and speed up the closed-loop response. To this end,  
 307  $N_p$  and  $\Gamma_u$  reset to their initial values whenever a new meal  
 308 disturbance is applied.

309 2) *Fuzzification:* At the fuzzification stage, the scaled val-  
 310 ues of the bound violation and the glucose change at the instant  
 311 where maximum violation occurs are fuzzified using the fuzzy  
 312 sets shown in Fig. 2. Particularly, if upper-bound violation oc-  
 313 curs, the scaled value  $A$  is specified as

$$A = \frac{y_{NN}(k+m) - y^u}{y^u} \quad (13)$$

314 If lower bound is violated, the scaled value  $B$  is specified as

$$B = \frac{y^l - y_{NN}(k+m)}{y^l} \quad (14)$$

315 where  $m(N_1 \leq m \leq N_p)$  is the instant at which maximum vio-  
 316 lation occurs. The definition of  $A$  and  $B$  guarantees positive value  
 317 if the corresponding bound is violated and negative otherwise.  
 318 The fuzzy set used for the fuzzification of the bound violation is  
 319 shown in Fig. 2(a), and consists of two membership functions,  
 320 namely: (G)ood denoted as G and (H)igh denoted as H. There-  
 321 fore, if the upper bound is violated, then  $A$  belongs to H and B  
 322 to G and vice versa.

323 The scaled value of glucose change at the instant where the  
 324 maximum violation occurs is defined as follows:

$$C = \frac{y_{NN}(k+m) - y_{NN}(k+m-1)}{y_{NN}(k+m)} \quad (15)$$

325 The scaled value of glucose change is transformed into a member  
 326 of fuzzy sets, using the fuzzy set shown in Fig. 2(b). This fuzzy  
 327 set consists of three membership functions: (P)ositive, (Z)ero,  
 328 and (N)egative.

329 3) *Inference Engine:* The base rules governing the tuning  
 330 guidelines are given in Table I. In this Table,  $\mu_r$  and  $\mu_{Np}$

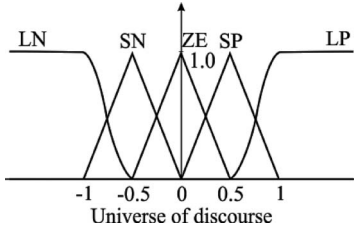


Fig. 3. Fuzzy set for the output of MPC parameters.

331 represent the rule output for  $N_p$  and  $\Gamma_u$ , respectively, while LN  
 332 (Large Negative), SN (Small Negative), ZE (Zero), SP (Small  
 333 Positive), and LP (Large Positive), are the output fuzzy sets  
 334 represented by sigmoid and triangular membership functions  
 335 as shown in Fig. 3. These functions are denoted as  $\mu_5$ ,  $\mu_4$ ,  
 336  $\mu_3$ ,  $\mu_2$ , and  $\mu_1$ , respectively. The base rules formulate the gen-  
 337 eral understanding of the effect of parameters  $N_p$  and  $\Gamma_u$   
 338 in closed-loop response. In general, according to simulation ex-  
 339 perience [20], increasing  $N_p$  at a fixed nonzero value of  $\Gamma_u$   
 340 results in a faster response with less overshoot. Furthermore,  
 341 reduction of  $\Gamma_u$  speeds up the response. We chose to increase  
 342  $N_p$  for both upper- and lower-bound violation, in order to pre-  
 343 vent from large overshoots in glucose response—which may  
 344 result in hyperglycaemic episodes—while speeding up the glu-  
 345 cose response to avoid hypoglycemic episodes. Moreover, since  
 346 reduction of  $\Gamma_u$  speeds up the response, parallel reduction of  $N_p$   
 347 should be avoided, because this would lead to more aggressive  
 348 control performance and might result to instability.

349 4) *Defuzzification*: At the defuzzification stage, the outputs  
 350 of the base rules are properly processed in order to produce crisp  
 351 values, which are used as factors to update the NMPC control pa-  
 352 rameters. The base rules of Table I, which are in linguistic form,  
 353 are expressed in mathematical form using a common fuzzy rule  
 354 operation [20]. Particularly, the AND command is transformed  
 355 into minimum operation. For example, the results of Rule 1 in  
 356 Table I can be written as follows:

$$\mu_{4,1}(\Gamma_u) = \min(\mu_H(A), \mu_G(B)) \quad (16)$$

$$\mu_{1,1}(N_p) = \min(\mu_H(A), \mu_G(B)) \quad (17)$$

358 where  $\mu_H(A)$  is the degree of membership of A in the fuzzy set  
 359 H and  $\mu_{j,i}(\bullet)$  denotes the membership degree of ( $\bullet$ ) to the  $j$ th  
 360 output membership function with respect to rule  $i$ . Therefore,  
 361 the center of area principle [32] is applied in order to produce the  
 362 correction factor  $\Gamma_u$ . For the prediction horizon, the correction  
 363 factor is calculated as

$$w_k(N_p) = \sum_{j=1}^{n_R} \sum_{i=1}^{n_f} \mu_{j,i}(N_p) \delta_i \quad (18)$$

364 where  $n_R$  and  $n_f$  represent the number of rules and the number  
 365 of membership functions, respectively, while  $\delta_i$  is the value for  
 366 the center location of the activated output membership function.  
 367 Since  $N_p$  is an integer, the correction factor is rounded to the  
 368 nearest integer.

### III. RESULTS AND DISCUSSION

369

In order to evaluate the performance and the robustness of the  
 designed IIAS, the UVa T1DM simulator [21] has been used.  
 The UVa T1DM simulator incorporates a modified version of  
 the meal model developed by Man *et al.* [22]–[24] to adapt for  
 T1DM subjects and insulin exogenous infusion [22]. In addition  
 to the patient model, the simulator incorporates a sensor-related  
 errors model to account for sensor noise and measurements'  
 errors and a model for the sc insulin pump. The UVa T1DM  
 simulator simulates a sufficiently large cohort of *in silico* sub-  
 jects in order to cover the wide variability observed among  
 diabetic population and serves as an *in silico* environment for  
 preclinical testing trial. In this paper, the proposed IIAS has been  
 tested with the ten adults' population available in the training  
 version of the UVa simulator. The ten patients are characterized  
 by a wide diversity in their parameters (e.g., body weight and  
 insulin sensitivity) and, therefore, can serve as small population  
 to evaluate the controller [8], [9].

The evaluation of the IIAS is performed in two stages: 1)  
 evaluation of the predictive performance of the personalized  
 glucose–insulin metabolism model; and 2) evaluation of the  
 controller considering several simulation scenarios.

#### A. Evaluation of the Personalized Glucose–Insulin Metabolism Model

Open-loop experiments were performed in order to generate  
 the data for the training and testing of the personalized glucose–  
 insulin metabolism models. Particularly, each *in silico* subject  
 was fed for one week, with 1) basal rate, which keeps the spe-  
 cific patient at its fasting state (provided by the UVa T1DM  
 simulator), 2) insulin bolus whenever carbohydrates were in-  
 gested (provided by the UVa T1DM simulator), and 3) various  
 meal profiles corresponding to breakfast, lunch, dinner, and two  
 snacks. In order to account for patient real life, meal times  
 and amounts values were randomly chosen within the follow-  
 ing ranges: {[6–8 A.M.], [12–2 P.M.], [4–4.30 P.M.], [6–8 P.M.],  
 [10–11 P.M.]} and {[40–60 g], [60–80 g], [0–10 g], [70–90 g],  
 and [0–10 g]}, respectively. Data corresponding to the first four  
 days were used for training the model, while the remaining three  
 days were used for its testing. The predictive performance of the  
 glucose–insulin metabolism model was evaluated considering a  
 prediction horizon equal to 30 min with a 5-min resolution.

Root-mean-squared error (RMSE) and correlation coefficient  
 (CC) corresponding to the testing dataset were calculated to  
 evaluate the performance of the glucose–insulin metabolism  
 model in terms of matching the predicted glucose with the orig-  
 inal ones. Furthermore, in order to evaluate the clinical accu-  
 racy of the glucose predictions and their effects on decisions  
 to avoid hypo- and hyperglycemic events, the continuous error  
 grid analysis [33] has been used. The estimates of point and  
 rate precision are combined in a single accuracy assessment for  
 each of the BG ranges: hypoglycemia, euglycemia, and hyper-  
 glycemia. To this end, the point error grid analysis (P-EGA)  
 and the rate error grid analysis (R-EGA) are combined in the  
 three clinically relevant regions of hypoglycemia, euglycemia,  
 and hyperglycemia. Clinically accurate glucose predictions are

TABLE II  
ERROR MATRIX COMBINING R-EGA AND P-EGA

		P-EGA										
		Hypoglycemia			Euglycemia			Hyperglycemia				
		A	D	E	A	B	C	A	B	C	D	E
R-EGA	A	69.61	13.26	0.00	75.35	4.99	0.02	38.00	4.80	0.00	0.00	0.00
	B	6.63	1.10	0.00	8.84	1.41	0.00	29.20	5.20	0.00	0.00	0.00
	uC	0.00	2.76	0.00	4.22	1.38	0.07	17.20	0.00	0.00	0.00	0.00
	IC	6.08	0.55	0.00	3.16	0.54	0.01	5.60	0.00	0.00	0.00	0.00
	uD	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
	ID	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
	uE	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
IE	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	
AR		76.24			90.61			77.20				
BE		6.08			9.29			22.80				
ER		17.68			0.00			0.00				

AR: Accurate readings, BE: Benign errors, ER: Erroneous errors.

424 considered to be within the zones A and B on both P-EGA and  
425 R-EGA. Clinically benign errors correspond to acceptable point  
426 accuracy (i.e., A or B P-EGA zones) and significant errors in  
427 rate accuracy (i.e., C, D, or E R-EGA zones), which are unlikely  
428 to lead to negative clinical consequences. Clinically significant  
429 errors are those that could lead to a negative clinical action and  
430 therapeutic consequences.

431 From both the RMSE (mean  $\pm$  standard deviation (SD): 15.67  
432  $\pm$  6.03) and CC (mean  $\pm$  SD: 0.78  $\pm$  0.16), it is obvious that  
433 the predicted glucose profile follows the original one. Moreover,  
434 the error matrix combining P-EGA and R-EGA, presented in  
435 Table II, shows that erroneous errors are observed in the range  
436 of hypoglycemia.

437 Although the proposed glucose–insulin metabolism model  
438 uses CMs for the simulation of sc insulin kinetics and glucose  
439 absorption from the gut, similarly with the UVa T1DM sim-  
440 ulator, it adopts a completely different approach based on the  
441 RNN to map plasma insulin to sc glucose. The latter consists of  
442 the most essential module of the model. The previously presented  
443 prediction accuracy assessment refers to primarily testing the  
444 RNN and its effective combination with the CMs. The predic-  
445 tive performance of the glucose–insulin metabolism model has  
446 been assessed in a previous study [25], and the superiority of the  
447 used RNN over a feedforward neural network (FNN) has been  
448 demonstrated [26], using real patient data.

#### 449 B. IAS Tuning

450 The IAS provides the estimated insulin infusion rates every  
451 5 min. Regarding the performance envelope, lower  $y^l$  and up-  
452 per  $y^u$  bounds were chosen to be constant and equal to 90 and  
453 140 mg/dl, respectively, corresponding to a rather narrow target  
454 range. Particularly, 90 mg/dl corresponds to the minimum BG  
455 level of optimal glucose control [21], while 140 mg/dl is the  
456 maximum 2-h postprandial BG level [8]. Moreover,  $LG$  and  
457  $HG$  were set to 70 and 180 mg/dl, respectively, since, in this  
458 paper, BG concentrations between 70 and 180 mg/dl are con-  
459 sidered to be within the target range for T1DM. The values of  
460 the weighting coefficients  $\Gamma_L, \Gamma_H$ , and  $\Gamma_e$  were chosen to be 10,

TABLE III  
IIAS TUNING

Weighting Coefficients				Prediction, minimum and control horizon		
$\Gamma_{uv}$	$\Gamma_L$	$\Gamma_H$	$\Gamma_e$	$P_w$	$N_1$	$N_c$
10	10	1	100	10	1	1
Limits of performance envelop (mg/dl)				Glucose target range (mg/dl)		Reference glucose (mg/dl)
$y^l$		$y^u$		$LG$	$HG$	$r$
90		140		70	180	110

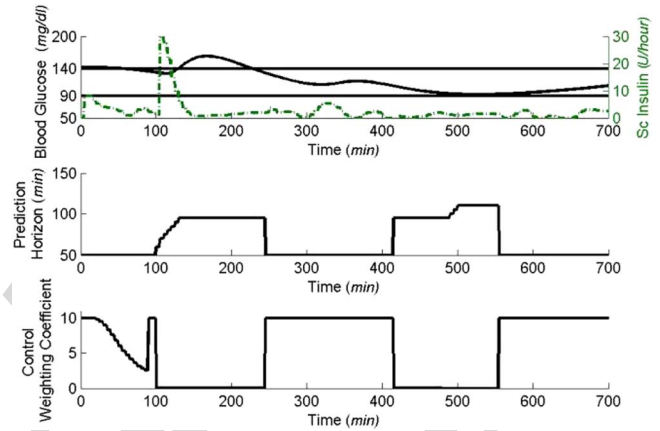


Fig. 4. Upper panel: Adult 5, sc insulin infusion rates (dashed-dotted line), BG data (solid line), limits of performance envelop [90–140 mg/dl] (dashed-line). Middle panel: Prediction horizon. Low panel: control weighting coefficient.

461 1, and 100, respectively. The rather large  $\Gamma_e$  value causes quite  
462 high insulin infusion rates, which are necessary to prevent hyper-  
463 glycemic episodes after meal ingestion. Furthermore,  $\Gamma_L$  is  
464 large enough to appropriately penalize for glucose predictions  
465 lower than 70 mg/dl and thus preventing from extremely high in-  
466 sulin infusion rates that would lead to hypoglycemic episodes.  
467 Parameter  $P_w$  is set to 10 corresponding to 50 min in order  
468 for the prediction horizon to account for sc insulin action. The  
469 control weighting coefficient  $\Gamma_{uv}$  is set to 10, which is high  
470 enough to ensure stability of the glucose controller.  $N_c$  is set to  
471 1 (its minimum possible value), corresponding to 5 min, in order  
472 to minimize on-line computation and  $N_1 = 1$  (see Section  
473 II-B). Moreover,  $u_{\min} = 0$  U/h while  $u_{\max} = 70$  U/h in accord-  
474 ance with the maximum allowable values for patients' safety  
475 and pump's hardware limitations [8]. The reference glucose  
476 level  $r$  is set to 110 mg/dl, which corresponds to the minimum  
477 value of the risk index. The numerical values of the parameters  
478 are summarized in Table III.

479 In order to clearly present the evolution of the prediction hori-  
480 zon  $N_p$  along with the control weighting coefficient  $\Gamma_u$  over  
481 time, the following simulation scenario has been studied: Adult  
482 5 was fed with 50 g at time 100 min. In Fig. 4, BG levels, sc  
483 insulin infusion rates along with prediction horizon, and control  
484 weighting coefficient are shown. As can be observed, the tuning  
485 algorithm does not always enter the triggered phase. It enters the  
486 triggered phase whenever there is danger for BG levels to ex-  
487 ceed the limits of the performance envelop (90–140 mg/dl), and

TABLE IV  
DAILY MEAL PROFILES

Day	1					2			
Meal Time (h)	07:00	12:00	16:00	18:00	23:00	07:30	13:00	18:30	
Meal Amounts (g)	45	70	0	5	80	5	40	85	60

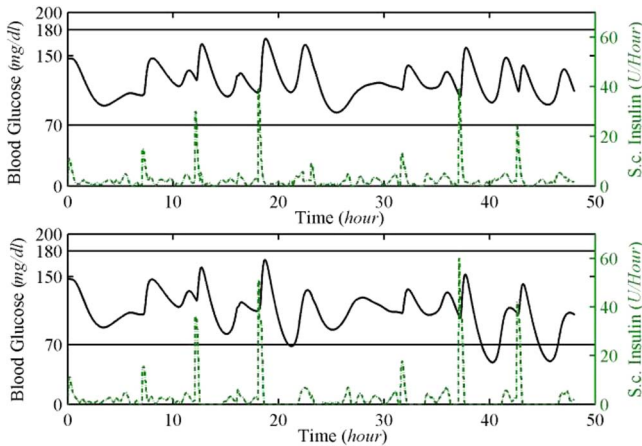


Fig. 5. Control results for Adult 3 under IIAS (upper panel) and fixed parameters NMPC (low panel). Estimated insulin infusion rates (dashed-dotted line), BG data (solid line), glucose target range [70–180 mg/dl].

488 appropriately updates the NMPC parameters, managing to reset  
489 and maintain glucose levels within the performance envelop.

### 490 C. Evaluation of the Controller—Simulation Scenarios

491 To evaluate IIAS’s performance under realistic conditions,  
492 several scenarios have been simulated. Particularly, the IIAS has  
493 been tested for its ability to handle meal disturbances, fasting  
494 conditions, interpatient variability, robustness against erroneous  
495 estimation of carbohydrates’ amount in ingested meals, and  
496 intraday variation in physiological parameters. Furthermore, in  
497 order to study the effectiveness of the tuning algorithm, two  
498 simulation scenarios have been studied: with (IIAS) and without  
499 (fixed parameter NMPC) the tuning algorithm.

500 1) *Evaluation of the IIAS Against Fixed Parameter NMPC:*  
501 Both controllers have been tested with the ten adults’ population.  
502 It should be noted that in the case of fixed parameter NMPC,  $N_p$   
503 and  $\Gamma_e$  are fixed over time and set both to 10. The simulation  
504 scenarios consider a two-day testing period with varying meal  
505 timings and amounts (see Table IV).

506 The superiority of the IIAS over fixed parameter NMPC is  
507 shown in Figs. 5 and 6. Fig. 5 presents the estimated sc insulin  
508 infusion rates along with the corresponding BG levels, when  
509 Adult 3 is fed with the two-day meal protocol and regulated  
510 using the IIAS (upper panel) and the fixed parameter NMPC  
511 (low panel), respectively. It should be noted that the controllers  
512 activate either the basal or the bolus action provided from the  
513 insulin pumps and hold the estimated insulin dose constant be-  
514 tween sampling instants (per 5 min). As shown in Fig. 5, the  
515 application of fixed parameter NMPC caused severe hypogly-  
516 caemic episodes, which are defined as BG levels lower than

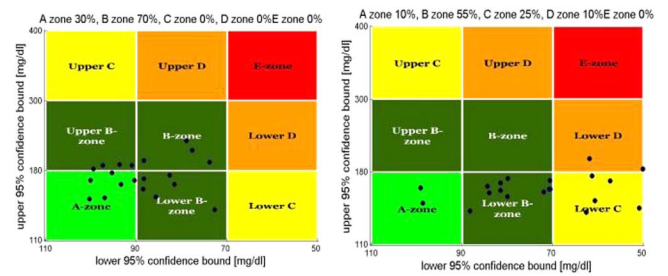


Fig. 6. CVGA for the ten adults of the Uva T1DM simulator. *left*: IIAS (30% in zone A and 70% in zone B). *Right*: NMPC (10% in zone A, 55% in zone B, 25% in zone C, and 10% in zone D).

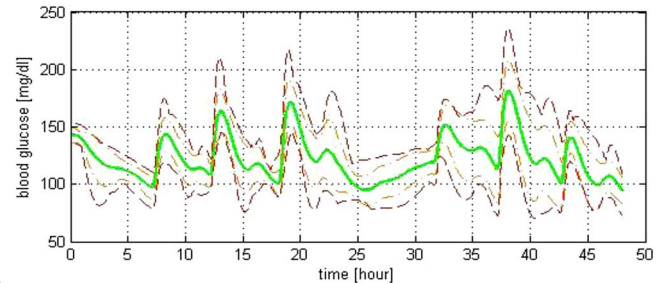


Fig. 7. BG trace for the ten adults of the Uva T1DM simulator when the IIAS is applied. Mean response (solid curve), SD (dashed-dotted curve), and min/max envelop (dashed curve).

60 mg/dl [9]. On the other hand, the IIAS managed to main- 517  
518 tain BG levels within the target range (70 --180 mg/dl), while  
519 achieving less fluctuations over time.

520 The control variability grid analysis (CVGA) [34], shown in  
521 Fig. 6, serves as a tool to evaluate the controllers with the en-  
522 tire population. Each point in the CVGA represents the lower and  
523 the upper bound of 95% confidence interval of BG data for  
524 one patient during one day. Zones A and B are considered to  
525 represent good glucose control. CVGA demonstrates that IIAS  
526 provides superior performance over the fixed parameter NMPC,  
527 managing to keep all the patients inside the zones A and B.  
528 Furthermore, the min/max envelop presented in Fig. 7 indicates  
529 that the BG levels for the hard-to-control patients are within  
530 the acceptable range 70–236 mg/dl, managing to avoid hypo-  
531 glycemic episodes and severe hyperglycemic episodes (above  
532 280 mg/dl).

533 Moreover, numerical metrics of average glycemia, percentage  
534 within the target range (70–180 mg/dl), risk associated with ex-  
535 treme glucose deviations [35] (low blood glucose index (LBGI),  
536 high blood glucose index (HBGI), and total risk index), are used  
537 to provide more details about the controller performance. In Ta-  
538 ble V, the obtained numerical results, when the IIAS is applied  
539 on all 10 patients, are presented. It can be seen that most of the  
540 time, BG levels are kept within the target range, while the risk  
541 indices (LBGI, HBGI, and total risk index) have low values,  
542 showing that tight glycemic control is achieved.

543 2) *Robustness to Meal Estimation Errors:* Since the pro-  
544 posed IIAS is informed about the carbohydrates amount of the  
545 upcoming meal, its ability to handle meal estimation errors is  
546 of utmost importance. To this end, the IIAS has been tested

TABLE V  
CONTROL PERFORMANCE OF THE IIAS AND THE OPEN-LOOP PREADJUSTED TREATMENT

Simulation scenario	mean BG Mean ( $\pm$ SD)	Pre meal BG Mean ( $\pm$ SD)	Post meal BG Mean ( $\pm$ SD)	% below target Mean ( $\pm$ SD)	% above target Mean ( $\pm$ SD)	% within target Mean ( $\pm$ SD)	LBG1 Mean ( $\pm$ SD)	HBGI Mean ( $\pm$ SD)	risk index Mean ( $\pm$ SD)
Accurate meal announcement (IIAS)	122.25 (9.06)	114.27 (12.31)	139.78 (9.19)	0 (0)	2.51 (2.76)	97.49 (2.76)	0.35 (0.35)	1.09 (0.64)	1.45 (0.66)
40% OEE (IIAS)	117.54 (7.91)	105.57 (8.99)	132.26 (12.68)	1.01 (1.51)	2.40 (3.13)	96.58 (2.83)	0.72 (0.34)	0.92 (0.62)	1.64 (0.66)
40% UEE (IIAS)	120.28 (10.61)	110.11 (11.13)	137.44 (14.30)	5.15 (5.07)	4.36 (4.43)	90.48 (6.66)	0.99 (0.71)	1.27 (0.86)	2.26 (1.10)
Intraday variation in physiological parameters (IIAS)	122.47 (7.58)	128.25 (15.79)	133.31 (15.42)	0.66 (0.87)	3.41 (3.25)	95.91 (3.61)	0.4 (0.27)	1.2 (0.65)	1.6 (0.71)
Open loop preadjusted treatment	130.50 (6.92)	124.4 (6.65)	145.16 (10.80)	1.14 (3.61)	3.68 (3.78)	95.17 (5.59)	0.30 (0.48)	1.65 (0.69)	1.96 (0.91)

547 against overestimation errors (OEE) and underestimation errors  
548 (UEE) up to 40%. Table V demonstrates the mean values and the  
549 SDs of the numerical metrics over the results obtained for the  
550 ten adults. Although certain hypoglycemic and hyperglycemic  
551 episodes occurred, none of them was severe. It is noteworthy  
552 that the IIAS is able to handle meal estimation errors and regu-  
553 late properly insulin infusion rate, in order to keep glucose  
554 within the target range most of the time.

555 3) *Robustness Against Intraday Variation in Physiological*  
556 *Parameters:* One of the critical challenges for a glucose con-  
557 trol algorithm is robustness against intraday variation in phys-  
558 iological parameters. In order to represent diurnal metabolic  
559 variations, time variation of the *in silico* patient-specific phys-  
560 iological parameters was considered, as drawn from a normal  
561 distribution with SD of 10%. This distribution was chosen to  
562 capture the expected variation in insulin sensitivity [36]. In Table  
563 V, the obtained numerical results over the ten adults are  
564 presented. The IIAS achieved good glucose control, managing  
565 to maintain BG levels within the acceptable range for 95.17%  
566 of the total time, avoiding severe hypoglycemic and hyper-  
567 glycemic episodes. Furthermore, the risk indices are low, prov-  
568 ing the IIAS' ability to handle intraday variation in physiological  
569 parameters.

#### 570 D. Comparison of the IIAS With Other Glucose Controllers

571 In order to prove the efficacy of the IIAS, its performance has  
572 been compared with that of other open-loop and closed-loop  
573 glucose controllers.

574 1) *Open-Loop Preadjusted Treatment:* The open-loop  
575 preadjusted treatment is supported by the UVa T1DM simulator.  
576 The ten *in silico* adults of the simulator followed a protocol of  
577 meals presented in Table IV. A matching insulin bolus and a  
578 basal rate were provided by the UVa T1DM simulator for each  
579 *in silico* adult and the results obtained by applying the open-  
580 loop preadjusted treatment are presented in Table V. It can be  
581 observed that the IIAS achieves better glucose control.

582 2) *Adaptive Basal Therapy:* Since the basal rate provided  
583 by the UVa T1DM simulator is nonoptimal, the IIAS has been  
584 compared with adaptive basal therapy [37]. The latter suggests  
585 adaptation of the basal rate as a gain multiplier based on the cur-

TABLE VI  
COMPARISON OF THE IIAS WITH THE ADAPTIVE BASAL THERAPY [37]

Controller	Hypo- percent (<60mg/dl)	Hyper- percent	Safe percent	risk index
IIAS	0.00 $\pm$ 0.00	0.60 $\pm$ 1.52	99.40 $\pm$ 1.52	0.99 $\pm$ 0.43
Adaptive Basal Therapy	0.5 $\pm$ 0.01	1.3 $\pm$ 0.03	98.2 $\pm$ 0.03	1.7 $\pm$ 0.59

586 rent CGM glucose value and its rate of change. Identical meals  
587 used in [37] provided input to the ten *in silico* adults, which were  
588 regulated by the IIAS. In particular, the ten *in silico* adults fol-  
589 lowed a one-day meal scenario of 40, 75, 60 g of carbohydrates  
590 at 7:00 A.M., 12:00 A.M., and 6:00 P.M., respectively. Results ob-  
591 tained from the application of the IIAS and the adaptive basal  
592 therapy are presented in Table VI in terms of hyperglycemia  
593 and severe hypoglycemia (<60 mg/dl) along with risk indices.  
594 It can be observed that the IIAS provides better glucose control  
595 performance.

596 3) *Artificial Pancreatic  $\beta$ -Cell Based on Zone-MPC:* In order  
597 to justify the use of the proposed nonlinear approach to  
598 improve glucose control, the IIAS has been compared with an ar-  
599 tificial pancreatic  $\beta$ -cell based on zone-MPC that uses mapped-  
600 input data and is adjusted automatically by linear difference  
601 personalized models [38]. The ten *in silico* adults followed the  
602 three meal scenario used in [38]—consisting of 75, 75, and 50 g  
603 of carbohydrates at 7 A.M., 1 P.M., and 8 P.M., respectively—and  
604 were regulated by the IIAS. The obtained results are presented  
605 in Table VII. It should be noted that no severe hypoglycemic  
606 (<60 mg/dl) and hyperglycemic episodes (>280 mg/dl) have  
607 been observed during the operation of the IIAS- and zone-MPC-  
608 based glucose controllers. As discussed in [38], a single severe  
609 hypoglycemic event occurred during the operation of the MPC  
610 with set point at 110 mg/dl. When the *in silico* adults were regu-  
611 lated by the IIAS, the mean glucose value was closer to the  
612 desired glucose level, while the average SD of the mean glucose  
613 value was lower, indicating lower variability in glucose con-  
614 trol performance among the *in silico* adults. Furthermore, lower



TABLE VII  
COMPARISON OF THE IIAS WITH THE ARTIFICIAL PANCREATIC B-CELL [38]

Controller	Mean Glucose	Hyper- percent
IIAS	117.61 ± 7.11	0.81 ± 2.05
Zone-MPC (bounds: 80-140 mg/dl) (Experiment 5 in [38])	152.00 ± 28.00	27.99 ± 20.51
Zone-MPC (bounds: 100-120 mg/dl) (Experiment 6 in [38])	141.00 ± 29.00	20.75 ± 19.45
MPC (set-point 110 mg/dl) (Experiment 7 in [38])	136.00 ± 29.00	17.54 ± 18.58

percentage of hyperglycemia was observed during the operation of the IIAS. The obtained improved glucose control performance is related to higher on-line computation.

Summarizing, the use of a data-driven model for the simulation of the blood glucose–insulin kinetics (real-time self-adaptive NN) permits personalization of the system and efficient handling of a changing environment. It is important to note that the incorporation of the RNN makes the model capable of simulating glucose–insulin kinetics taking into account patient specific information related to ingested carbohydrates, sc insulin infusion rate, and glucose records from CGMS that are usually available in clinical practice. The metabolic behavior of a specific patient is captured through the real-time update of the RNN’s weights. Whenever a new glucose measurement is applied to the model, the RNN’s weights are appropriately adapted in order to adjust to the new metabolic behavior. According to above, the RNN consists the most essential module of the personalized glucose–insulin metabolism model. Thus, the similarities of the latter with the UVa T1DM simulator regarding the use of CMs for the sc insulin kinetics and the glucose absorption from the gut do not limit the reliability of the presented assessment of the IIAS performance. This is of particular importance since the IIAS has demonstrated robustness against intraday variation in physiological parameters. Moreover, the tuning algorithm for the real-time update of the NMPC control parameters greatly improved controller’s performance, demonstrating its importance toward the tuning of glucose controllers based on MPC.

Clinical evaluation of the IIAS on real T1DM patients is in progress. Future research activities are focused on the optimization of the proposed IIAS and its complete integration into a telecommunication platform for the efficient management and treatment of patients with T1DM [39].

#### IV. CONCLUSION

A novel IIAS based on NMPC has been proposed in order to estimate optimal insulin infusion rates. The proposed approach introduces 1) a personalized model based on the combined use of CMs and an RNN for the simulation of glucose–insulin metabolism and 2) an automatic algorithm for the on-line adaptation of NMPC parameters. The performance of the IIAS has been *in silico* evaluated using the ten adults’ population, available in the training version of the UVa T1DM simulator. The obtained results demonstrate that the proposed IIAS is robust

with respect to its ability to handle various conditions characterized by sensor errors, lags, meal disturbances, large meal estimation errors, interpatient variability, and intraday variation in physiological parameters.

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# An Insulin Infusion Advisory System Based on Autotuning Nonlinear Model-Predictive Control

Konstantia Zarkogianni, Andriani Vazeou, Stavroula G. Mougiakakou, *Member, IEEE*, Aikaterini Prountzou, and Konstantina S. Nikita\*, *Senior Member, IEEE*

**Abstract**—This paper aims at the development and evaluation of a personalized insulin infusion advisory system (IIAS), able to provide real-time estimations of the appropriate insulin infusion rate for type 1 diabetes mellitus (T1DM) patients using continuous glucose monitors and insulin pumps. The system is based on a nonlinear model-predictive controller (NMPC) that uses a personalized glucose–insulin metabolism model, consisting of two compartmental models and a recurrent neural network. The model takes as input patient’s information regarding meal intake, glucose measurements, and insulin infusion rates, and provides glucose predictions. The predictions are fed to the NMPC, in order for the latter to estimate the optimum insulin infusion rates. An algorithm based on fuzzy logic has been developed for the online adaptation of the NMPC control parameters. The IIAS has been *in silico* evaluated using an appropriate simulation environment (UVa T1DM simulator). The IIAS was able to handle various meal profiles, fasting conditions, interpatient variability, intraday variation in physiological parameters, and errors in meal amount estimations.

**Index Terms**—Artificial pancreas (AP), autotuning model-predictive control, personalized model, type I diabetes mellitus (T1DM).

## I. INTRODUCTION

INSULIN-dependent diabetes mellitus is a metabolic disorder, characterized by the disability of the body to regulate blood glucose (BG) levels. Particularly, it is an autoimmune disease in which the  $\beta$ -cells of the pancreas are destroyed, resulting in the absence of insulin secretion. Chronic elevation

of BG level leads to damage of blood vessels (angiopathy), resulting in serious long-term complications, such as blindness, neuropathy, heart disease, and kidney failure. According to the diabetes control and complications trial [1], the aforementioned complications can be reduced by intensive glycemic control, which involves regular glucose measurements and exogenous insulin administration. Latest advances in technology have led to the development of continuous glucose monitors (CGMs) that provide subcutaneous (sc) glucose measurements at a high frequency [2], and insulin pumps for continuous sc insulin infusion.

The experience with CGMs and insulin pumps, along with advances in computational algorithms for the automatic estimation and adjustment of appropriate insulin infusion rates makes the development of a wearable artificial pancreas (AP) feasible [3]. Closed-loop glucose control systems can be categorized according to the way mealtime insulin delivery is handled. In “fully closed-loop” mode, insulin is delivered without information about the time or size of the meal. In “semiclosed-loop” control, the controller is provided with information regarding the meal size and generates advice on prandial insulin. A significant benefit to controller performance can be obtained, when meal information is provided. Although a wide range of algorithms have been proposed [4], the most common approaches are based on proportional integral derivative controller [5], [6], and model-predictive controller (MPC) [7]–[16]. MPC (linear and nonlinear) seems to be the most appropriate for the development of AP, since it is able to handle problems related to 1) high nonlinearity of the glucose–insulin metabolism, caused by saturation and inhibition effects evidenced by chemical substrates and hormones involved in enzyme dynamics and hormonal control effects, 2) time delays in sc–sc route due to the delayed effect of infused sc insulin and food intake to the blood and, consequently, of glucose diffusion from the blood to the sc space, and the lag time between sc glucose value and glucose sensor (in the case of sensors based on microdialysis or microperfusion), and 3) noise to the sc glucose measurements. The models used to develop glucose controllers based on linear MPC are usually discrete linearized state-space models obtained from the average original nonlinear patient’s model, which serves as the *in silico* T1DM patient for the evaluation of the glucose controllers [7], [8], [12]. However, such an approach would suffer from the lack of personalization [4] and from dependencies between the predictive model integrated in the glucose controller and the *in silico* patient model, thus limiting the reliability of the *in silico* evaluation of the controller. A model-predictive iterative learning control has been proposed based on

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80 a data-driven linear autoregressive exogenous model (ARX) [9].  
 81 Although this model cannot describe accurately the real relation-  
 82 ship between glucose and insulin in T1DM, the proposed  
 83 control law performed well, especially in the case of repetitive  
 84 diets. Meal detection and meal size estimation algorithms have  
 85 been developed to improve meal glucose disturbance rejection  
 86 when incoming meals are not announced [11]. Furthermore,  
 87 several attempts have been made toward the development of  
 88 glucose controllers based on nonlinear model-predictive control  
 89 (NMPC), [10], [13] [14] and the effectiveness of the NMPC over  
 90 the linear MPC has been studied [14]. The models used to de-  
 91 velop glucose controllers based on NMPC are usually derived by  
 92 compartmentalizing the various physiological components in-  
 93 volved in the human metabolic process [10], [14]. The fact that  
 94 some of the endocrine processes affecting glucose metabolism  
 95 are still not fully understood may limit the effectiveness of these  
 96 controllers. Moreover, experiments on real patients using NMPC  
 97 have been performed [14]–[16]. Clinical trials have been con-  
 98 ducted to investigate whether the closed-loop insulin delivery  
 99 could control overnight BG [17], [18].

100 A very important issue toward the implementation of MPC  
 101 is its tuning. Traditionally, the MPC has a set of tuning pa-  
 102 rameters, which add flexibility and influence its performance  
 103 and stability. Usually, their values are adjusted either via trial  
 104 and error procedures or by following general tuning guide-  
 105 lines [19]. Because of the overlapping effect of the MPC pa-  
 106 rameters, trial and error is a rather cumbersome task [20]. Fur-  
 107 thermore, systematic approaches following tuning guidelines  
 108 cannot be implemented online by control operators because the  
 109 glucose metabolism is subject to severe disturbances and chang-  
 110 ing operating conditions. In order to overcome the aforemen-  
 111 tioned problems, an on-line adaptive strategy for MPC based  
 112 on fuzzy logic has been proposed [20], which enables auto-  
 113 matic tuning of the parameters and results in good control  
 114 performance.

115 To account for the highly nonlinear nature of the gluco-regu-  
 116 latory system, this study aims at the design, development, and  
 117 evaluation of a novel Insulin Infusion Advisory System (IIAS)  
 118 based on NMPC, which makes use of a new personalized model  
 119 for the simulation of glucose–insulin metabolism in type 1 dia-  
 120 betes mellitus (T1DM). To address the day-to-day variability in  
 121 the glucose dynamics of a T1DM individual and the interpatient  
 122 variability, the proposed personalized approach incorporates a  
 123 data-driven model, able to capture the glucose metabolic behav-  
 124 ior taking into account patient specific information. Moreover,  
 125 an automatic algorithm for the adaptation of the NMPC’s control  
 126 parameters over time is introduced. The IIAS has been evalu-  
 127 ated using the UVa-type T1DM simulator [21], which has been  
 128 approved by the Food and Drug Administration as a substitute  
 129 for animals’ trial in preclinical testing of closed-loop AP control  
 130 algorithms.

## 131 II. METHODOLOGY

132 The proposed IIAS comprises two modules: 1) the person-  
 133 alized glucose–insulin metabolism model; and 2) the NMPC.  
 134 These modules along with the automatic algorithm for on-

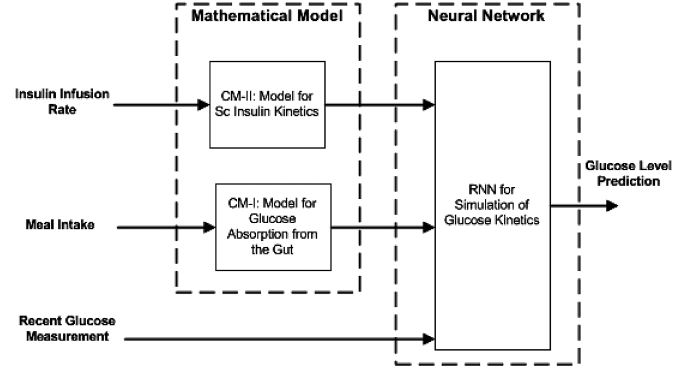


Fig. 1. Outline of the personalized glucose–insulin metabolism model used by the IIAS.

line tuning of NMPC control parameters are described in the following.

### A. Personalized Glucose–Insulin Metabolism Model

In order to provide the controller with glucose predictions ahead in time, a personalized glucose–insulin metabolism model (see Fig. 1) has been developed. The model is based on the combined use of a mathematical model (MM) module and a neural network (NN) module. The MM module consists of two Compartmental Models (CMs), which simulate sc insulin kinetics and glucose absorption into the blood from the gut, respectively, while the NN module incorporates a recurrent neural network (RNN), which models the patient’s glucose kinetics. Information regarding recent sc insulin infusion rate and meal intake are fed to the MM module. CMs’ outputs along with the recent sc glucose measurement are applied to the RNN that provides glucose predictions.

1) *CM for sc Insulin Kinetics*: Following an sc insulin injection, the rate of appearance of insulin in plasma [ $R_i(t)$ ] is described by a linear CM [22]:

$$\dot{I}_{sc1}(t) = -(k_d + k_{a1}) \cdot I_{sc1}(t) + u(t), \quad I_{sc1}(0) = I_{sc1ss} \quad (1)$$

$$\dot{I}_{sc2}(t) = k_d \cdot I_{sc1}(t) - k_{a2} \cdot I_{sc2}(t), \quad I_{sc2}(0) = I_{sc2ss} \quad (2)$$

$$R_i(t) = k_{a1} \cdot I_{sc1}(t) + k_{a2} \cdot I_{sc2}(t) \quad (3)$$

where  $I_{sc1}$  and  $I_{sc2}$  represent the amount of nonmonomeric and monomeric insulin in the sc space, respectively,  $u(t)$  (pmol/kg/min) is the exogenous insulin infusion rate,  $k_d$  (0.0164 min<sup>-1</sup>) is the rate constant of insulin dissociation, and  $k_{a1}$  (0.0018 min<sup>-1</sup>) and  $k_{a2}$  (0.0182 min<sup>-1</sup>) are the rate constants of nonmonomeric and monomeric insulin absorption, respectively.

2) *CM for Glucose Absorption From the Gut*: The physiological model of glucose intestinal absorption is a three-compartment nonlinear model with two compartments representing the stomach (solid and liquid phases) and the third compartment representing the intestine [22], [24]. The model assumes a constant rate of the intestinal absorption

167 but describes gastric emptying rate to be dependent on the  
168 total amount of nutrient in the stomach. Following a meal, the  
169 appearance rate of glucose in plasma,  $Ra$  (in mg/kg/min), is  
170 estimated by the following differential equations:

$$Q_{sto}(t) = Q_{sto1}(t) + Q_{sto2}(t), \quad Q_{sto}(0) = 0 \quad (4)$$

$$\dot{Q}_{sto1}(t) = -k_{gri} \cdot Q_{sto1}(t) + D \cdot d(t), \quad Q_{sto1}(0) = 0 \quad (5)$$

$$\dot{Q}_{sto2}(t) = -k_{empt}(Q_{sto}) \cdot Q_{sto2}(t) + k_{sto} \cdot Q_{sto1}(t),$$

$$Q_{sto2}(0) = 0 \quad (6)$$

$$\dot{Q}_{gut} = -k_{abs} \cdot Q_{gut}(t) + k_{empt}(Q_{sto}) \cdot Q_{sto2}(t),$$

$$Q_{gut}(0) = 0 \quad (7)$$

$$Ra(t) = \frac{f \cdot k_{abs} \cdot Q_{gut}(t)}{BW}, \quad Ra(0) = 0 \quad (8)$$

171 where  $Q_{sto}$  (in mg) is the amount of glucose in the stomach  
172 ( $Q_{sto1}$ , solid and  $Q_{sto2}$ , liquid phase),  $Q_{gut}$  (in mg) is the  
173 glucose mass in the intestine,  $k_{gri}$  ( $0.0558 \text{ min}^{-1}$ ) is the rate  
174 of grinding,  $k_{empt}(Q_{sto})$  ( $\text{min}^{-1}$ ) is the rate constant of gastric  
175 emptying, which is a nonlinear function of  $Q_{sto}$  [22], and  
176  $k_{abs}$  ( $0.057 \text{ min}^{-1}$ ) is the rate constant of intestinal absorption.  
177 Moreover,  $f$  (0.90),  $D$  (in mg) and  $BW$  (in kg) represent the  
178 fraction of intestinal absorption which appears in plasma, the  
179 amount of ingested glucose, and the body weight, respectively.

180 3) *RNN*: The use of the RNN toward the development of  
181 glucose–insulin metabolism model has been studied and its ability  
182 to accurately simulate glucose kinetics taking into account  
183 previous insulin and meal intakes, along with recent glucose  
184 levels, has been proven [25].

185 The RNN used in the proposed personalized glucose–insulin  
186 metabolism model is a fully connected multilayered perceptron  
187 NN with two recurrent loops, whose initial weights are set to  
188 unity [27], [28]. Subcutaneous glucose levels are considered  
189 as the state variable, while the rate of appearance of insulin in  
190 plasma and the glucose absorption into the blood from the gut  
191 as external inputs. Future glucose predictions are calculated as

$$y_{NN}(k+1) = y_{NN}(k) + RNN(y_{NN}(k), R_{\alpha}(k+1), R_i(k)) \quad (9)$$

192 where  $y_{NN}(k+1)$  and  $y_{NN}(k)$  are the sc glucose level predic-  
193 tions at instant  $k+1$  and  $k$ , respectively. The RNN is trained us-  
194 ing the Real-Time Recurrent Learning (RTRL) algorithm [29].  
195 RTRL is a sequential, error-correction learning-based algorithm,  
196 which allows the RNN to update the weights while operating.  
197 The teacher-force version of the RTRL [29] has been applied,  
198 according to which the RNN replaces the previous glucose level  
199 prediction with the corresponding glucose level value, when  
200 available, in order to produce future predictions. During the op-  
201 eration of the IIAS, the RNN's weights are updated based on  
202 the RTRL algorithm, whenever a new glucose measurement is  
203 applied. This effectively enables the adaptation of the glucose–  
204 insulin metabolism model to the special characteristics of the  
205 patient and to the diurnal variation of the glucose metabolism.  
206 Thus, the on-line training of the RNN ensures its stable perfor-  
207 mance for the entire input space.

## B. NMPC

208

209 As already mentioned, the NMPC uses a model that provides  
210 estimates of the future outputs of the system to be controlled. The  
211 NMPC is based on an optimizer, which computes at each sam-  
212 ple time future control movements based on the minimization  
213 of an appropriate cost function. Particularly, at each instant: 1)  
214 future outputs  $y_{NN}(k+i)$ ,  $i = N_1, \dots, N_p$  are generated by the  
215 prediction model; 2) a cost function of the future control move-  
216 ments is minimized providing a set of future control signals;  
217 and 3) only the first element of the suggested control sequence  
218 is applied to the system. The procedure is repeated at the next  
219 instant.

220 The definition of the cost function is critical to controller's  
221 performance. The cost function used in this paper [see (10)],  
222 consists of the standard MPC formulated cost function [30] and  
223 one penalty term [31]. Particularly, in (10), first and second  
224 terms represent the deviations of the glucose predictions from  
225 the reference glucose level  $r$ , and the changes in future insulin  
226 infusion rates, respectively, while the third term consists of two  
227 penalty terms, which add soft constraints ( $LG \leq y_{NN}(k+i) \leq$   
228  $HG$ ) to the optimization problem. The penalty terms increase  
229 the cost function whenever the glucose predictions are outside  
230 the acceptable range determined by the lowest ( $LG$ ) and the  
231 highest ( $HG$ ) desired glucose level. In (10),  $N_p$  is the prediction  
232 horizon,  $N_1$  is the minimum prediction horizon,  $N_c$  is the control  
233 horizon, and  $\Gamma_e$  and  $\Gamma_u$  are the prediction and control weighting  
234 coefficients, respectively, while  $\Gamma_L, \Gamma_H$  are penalty coefficients:

$$J = \Gamma_e \sum_{i=N_1}^{N_p} (y_{NN}(k+i) - r)^2 + \Gamma_u \sum_{j=0}^{N_c} \Delta u^2(k+j)$$

$$+ \sum_{i=N_1}^{N_p} \left[ \Gamma_L [\min(0, y_{NN}(k+i) - LG)]^2 \right.$$

$$\left. + \Gamma_H [\min(0, HG - y_{NN}(k+i))]^2 \right] \quad (10)$$

235 where

$$\Delta u(k) = u(k) - u(k-1). \quad (11)$$

236 The cost function is minimized, subject to the constraints

$$u_{\min} \leq u(k) \leq u_{\max}. \quad (12)$$

237 Regarding the values of the aforementioned parameters,  $N_p$  is  
238 usually chosen to encompass all the response, which is signifi-  
239 cantly affected by the current control signal (sc insulin infusion).  
240 If there is no evidence about the dead time,  $N_1 = 1$ . The choice  
241 of  $N_c$  is usually based on a compromise between good glucose  
242 control performance and minimization of on-line computation.  
243 Furthermore, the selection of  $r, LG, HG, \Gamma_L,$  and  $\Gamma_H$  is based  
244 on a compromise between ability to handle high glucose lev-  
245 els (caused by meal disturbances) and simultaneously prevent  
246 high values of insulin infusion rates, which would cause severe  
247 hypoglycaemic episodes.

248 In this paper, an automatic tuning algorithm, similar to the  
249 one proposed in [20], is adopted for the on-line update of the  
250 parameters  $N_p$  and  $\Gamma_u$ . These parameters play an important role

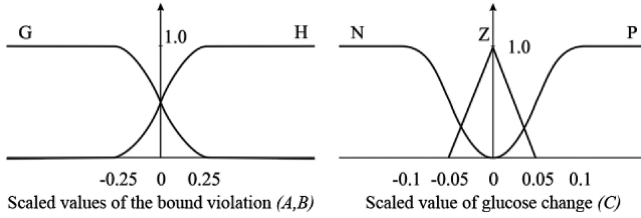


Fig. 2. Fuzzy sets for (a) bound violation and (b) bound violation rate.

251 to the controller's performance and stability. Although the time  
 252 to the peak action of sc insulin is considered to be 50 min, the  
 253 prediction horizon of 50 min is not always optimal, especially in  
 254 the presence of meal disturbances where glucose levels change  
 255 rapidly. This is of particular importance, since the sc glucose  
 256 measurements are subject to inaccuracies and there are lags  
 257 between the sc and the BG levels. The prediction weighting  
 258 coefficient  $\Gamma_e$  is chosen to be constant in order to avoid simul-  
 259 taneous increase of  $N_p$  and  $\Gamma_e$ , which would increase on-line  
 260 computation for the minimization of the cost function (10).

### 261 C. On-Line Tuning Algorithm of the NMPC Control Parameters

262 In order for the IIAS to rapidly reject meal disturbances  
 263 and maintain postprandial glucose levels within the acceptable  
 264 range, an automatic tuning algorithm has been developed. The  
 265 tuning technique adapts on-line the NMPC control parameters  
 266 in order to steer the closed-loop glucose response to satisfy pre-  
 267 set time-domain specifications, which are provided by the user  
 268 in the form of vectors of upper and lower bounds  $y^u$  and  $y^l$ ,  
 269 respectively. The new values of the NMPC control parameters  
 270 are determined by fuzzy logic rules.

271 1) *Overview of the Adaptation Algorithm:* The proposed  
 272 tuning method consists of two phases: the observation phase  
 273 and the triggered phase. In the former, the future glucose profile  
 274 is predicted, through the minimization of (10), by applying fixed  
 275 values to the prediction horizon  $P_w$  and the control weighting  
 276 coefficient  $\Gamma_{uw}$ . The obtained glucose profile is checked against  
 277 the performance envelope. In case a bound violation occurs, the  
 278 algorithm enters the triggered phase, otherwise the calculated  
 279 insulin infusion rate is applied to the system and the whole pro-  
 280 cedure is repeated at the next instant. Particularly, at each instant  
 281  $k$ , the steps of the tuning algorithm are as follows.

282 *Step 1.* Produce future glucose profile using fixed NMPC  
 283 control parameters through the minimization of the cost function  
 284 (10). The calculated insulin infusion rate at this step is not  
 285 applied to the patient.

286 *Step 2.* Check whether the predicted glucose profile, exceeds  
 287 the limits of the performance envelope, i.e.,  $y^u$  and  $y^l$ . If the  
 288 limits are not exceeded, go to step 8.

289 *Step 3.* Determine the corresponding glucose prediction and  
 290 the instant at which maximum bound violation occurs. Let this  
 291 be at instant  $k + m$ .

292 *Step 4.* Calculate the scaled values of the bound violation  
 293 ( $A$ ,  $B$ ), and the glucose change ( $C$ ) at instant  $k + m$ .

294 *Step 5.* Determine the degree of membership of  $A$ ,  $B$ , and  $C$   
 295 with respect to membership functions presented in Fig. 2.

TABLE I  
 BASE RULES OF THE TUNING ALGORITHM

No.	Rule	Result of $\Gamma_u$	Result of $N_p$
R1	If $A$ is H and $B$ is G	Then $\mu_r$ is SN	Then $\mu_{Np}$ is LP
R2	If $A$ is G and $B$ is H	Then $\mu_r$ is LN	Then $\mu_{Np}$ is LP
R3	If $A$ is G and $B$ is G	Then $\mu_r$ is ZE	Then $\mu_{Np}$ is SN
R4	If $A$ is H and $C$ is P	Then $\mu_r$ is LN	Then $\mu_{Np}$ is SP
R5	If $A$ is H and $C$ is Z	Then $\mu_r$ is SP	Then $\mu_{Np}$ is SN
R6	If $A$ is H and $C$ is N	Then $\mu_r$ is ZE	Then $\mu_{Np}$ is ZE
R7	If $B$ is H and $C$ is P	Then $\mu_r$ is SN	Then $\mu_{Np}$ is ZE
R8	If $B$ is H and $C$ is Z	Then $\mu_r$ is SP	Then $\mu_{Np}$ is SN
R9	If $B$ is H and $C$ is N	Then $\mu_r$ is ZE	Then $\mu_{Np}$ is SP

296 *Step 6.* Calculate the correction factors  $[w_k(N_p), w_k(\Gamma_u)]$ .

297 *Step 7.* Set the new parameters values as

$$298 N_{p,k} = N_{p,\text{previous}} + w_k(N_p) \quad \text{and} \quad \Gamma_{u,k} = \Gamma_{u,\text{previous}} \\ 299 (1 + w_k(\Gamma_u)), \text{ where } N_{p,\text{previous}} \text{ and } \Gamma_{u,\text{previous}} \text{ are calculated} \\ 300 \text{ during the previous triggered phase of the tuning algorithm.}$$

301 *Step 8.* Compute and apply the sc insulin infusion rate. Pro-  
 302 ceed to the next instant  $k + 1$  and go to step 1.

303 The initial values of  $N_p$  and  $\Gamma_u$  are set to  $P_w$  and  $\Gamma_{uw}$ , re-  
 304 spectively. In the presence of a meal disturbance, the control  
 305 parameters are appropriately updated in order to reduce the  
 306 overshoot and speed up the closed-loop response. To this end,  
 307  $N_p$  and  $\Gamma_u$  reset to their initial values whenever a new meal  
 308 disturbance is applied.

309 2) *Fuzzification:* At the fuzzification stage, the scaled val-  
 310 ues of the bound violation and the glucose change at the instant  
 311 where maximum violation occurs are fuzzified using the fuzzy  
 312 sets shown in Fig. 2. Particularly, if upper-bound violation oc-  
 313 curs, the scaled value  $A$  is specified as

$$A = \frac{y_{NN}(k+m) - y^u}{y^u} \quad (13)$$

314 If lower bound is violated, the scaled value  $B$  is specified as

$$B = \frac{y^l - y_{NN}(k+m)}{y^l} \quad (14)$$

315 where  $m(N_1 \leq m \leq N_p)$  is the instant at which maximum vio-  
 316 lation occurs. The definition of  $A$  and  $B$  guarantees positive value  
 317 if the corresponding bound is violated and negative otherwise.  
 318 The fuzzy set used for the fuzzification of the bound violation is  
 319 shown in Fig. 2(a), and consists of two membership functions,  
 320 namely: (G)ood denoted as G and (H)igh denoted as H. There-  
 321 fore, if the upper bound is violated, then  $A$  belongs to H and B  
 322 to G and vice versa.

323 The scaled value of glucose change at the instant where the  
 324 maximum violation occurs is defined as follows:

$$C = \frac{y_{NN}(k+m) - y_{NN}(k+m-1)}{y_{NN}(k+m)} \quad (15)$$

325 The scaled value of glucose change is transformed into a member  
 326 of fuzzy sets, using the fuzzy set shown in Fig. 2(b). This fuzzy  
 327 set consists of three membership functions: (P)ositive, (Z)ero,  
 328 and (N)egative.

329 3) *Inference Engine:* The base rules governing the tuning  
 330 guidelines are given in Table I. In this Table,  $\mu_r$  and  $\mu_{Np}$



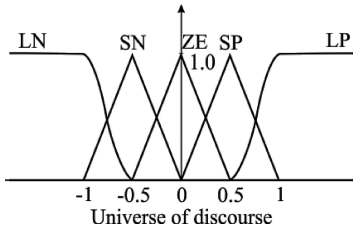


Fig. 3. Fuzzy set for the output of MPC parameters.

331 represent the rule output for  $N_p$  and  $\Gamma_u$ , respectively, while LN  
 332 (Large Negative), SN (Small Negative), ZE (Zero), SP (Small  
 333 Positive), and LP (Large Positive), are the output fuzzy sets  
 334 represented by sigmoid and triangular membership functions  
 335 as shown in Fig. 3. These functions are denoted as  $\mu_5$ ,  $\mu_4$ ,  
 336  $\mu_3$ ,  $\mu_2$ , and  $\mu_1$ , respectively. The base rules formulate the gen-  
 337 eral understanding of the effect of parameters  $N_p$  and  $\Gamma_u$   
 338 in closed-loop response. In general, according to simulation ex-  
 339 perience [20], increasing  $N_p$  at a fixed nonzero value of  $\Gamma_u$   
 340 results in a faster response with less overshoot. Furthermore,  
 341 reduction of  $\Gamma_u$  speeds up the response. We chose to increase  
 342  $N_p$  for both upper- and lower-bound violation, in order to pre-  
 343 vent from large overshoots in glucose response—which may  
 344 result in hyperglycaemic episodes—while speeding up the glu-  
 345 cose response to avoid hypoglycemic episodes. Moreover, since  
 346 reduction of  $\Gamma_u$  speeds up the response, parallel reduction of  $N_p$   
 347 should be avoided, because this would lead to more aggressive  
 348 control performance and might result to instability.

349 4) *Defuzzification*: At the defuzzification stage, the outputs  
 350 of the base rules are properly processed in order to produce crisp  
 351 values, which are used as factors to update the NMPC control pa-  
 352 rameters. The base rules of Table I, which are in linguistic form,  
 353 are expressed in mathematical form using a common fuzzy rule  
 354 operation [20]. Particularly, the AND command is transformed  
 355 into minimum operation. For example, the results of Rule 1 in  
 356 Table I can be written as follows:

$$\mu_{4,1}(\Gamma_u) = \min(\mu_H(A), \mu_G(B)) \quad (16)$$

$$\mu_{1,1}(N_p) = \min(\mu_H(A), \mu_G(B)) \quad (17)$$

358 where  $\mu_H(A)$  is the degree of membership of A in the fuzzy set  
 359 H and  $\mu_{j,i}(\bullet)$  denotes the membership degree of ( $\bullet$ ) to the  $j$ th  
 360 output membership function with respect to rule  $i$ . Therefore,  
 361 the center of area principle [32] is applied in order to produce the  
 362 correction factor  $\Gamma_u$ . For the prediction horizon, the correction  
 363 factor is calculated as

$$w_k(N_p) = \sum_{j=1}^{n_R} \sum_{i=1}^{n_f} \mu_{j,i}(N_p) \delta_i \quad (18)$$

364 where  $n_R$  and  $n_f$  represent the number of rules and the number  
 365 of membership functions, respectively, while  $\delta_i$  is the value for  
 366 the center location of the activated output membership function.  
 367 Since  $N_p$  is an integer, the correction factor is rounded to the  
 368 nearest integer.

### III. RESULTS AND DISCUSSION

369

In order to evaluate the performance and the robustness of the  
 designed IIAS, the UVa T1DM simulator [21] has been used.  
 The UVa T1DM simulator incorporates a modified version of  
 the meal model developed by Man *et al.* [22]–[24] to adapt for  
 T1DM subjects and insulin exogenous infusion [22]. In addition  
 to the patient model, the simulator incorporates a sensor-related  
 errors model to account for sensor noise and measurements'  
 errors and a model for the sc insulin pump. The UVa T1DM  
 simulator simulates a sufficiently large cohort of *in silico* sub-  
 jects in order to cover the wide variability observed among  
 diabetic population and serves as an *in silico* environment for  
 preclinical testing trial. In this paper, the proposed IIAS has been  
 tested with the ten adults' population available in the training  
 version of the UVa simulator. The ten patients are characterized  
 by a wide diversity in their parameters (e.g., body weight and  
 insulin sensitivity) and, therefore, can serve as small population  
 to evaluate the controller [8], [9].

The evaluation of the IIAS is performed in two stages: 1)  
 evaluation of the predictive performance of the personalized  
 glucose–insulin metabolism model; and 2) evaluation of the  
 controller considering several simulation scenarios.

#### A. Evaluation of the Personalized Glucose–Insulin Metabolism Model

Open-loop experiments were performed in order to generate  
 the data for the training and testing of the personalized glucose–  
 insulin metabolism models. Particularly, each *in silico* subject  
 was fed for one week, with 1) basal rate, which keeps the spe-  
 cific patient at its fasting state (provided by the UVa T1DM  
 simulator), 2) insulin bolus whenever carbohydrates were in-  
 gested (provided by the UVa T1DM simulator), and 3) various  
 meal profiles corresponding to breakfast, lunch, dinner, and two  
 snacks. In order to account for patient real life, meal times  
 and amounts values were randomly chosen within the follow-  
 ing ranges: {[6–8 A.M.], [12–2 P.M.], [4–4.30 P.M.], [6–8 P.M.],  
 [10–11 P.M.]} and {[40–60 g], [60–80 g], [0–10 g], [70–90 g],  
 and [0–10 g]}, respectively. Data corresponding to the first four  
 days were used for training the model, while the remaining three  
 days were used for its testing. The predictive performance of the  
 glucose–insulin metabolism model was evaluated considering a  
 prediction horizon equal to 30 min with a 5-min resolution.

Root-mean-squared error (RMSE) and correlation coefficient  
 (CC) corresponding to the testing dataset were calculated to  
 evaluate the performance of the glucose–insulin metabolism  
 model in terms of matching the predicted glucose with the orig-  
 inal ones. Furthermore, in order to evaluate the clinical accu-  
 racy of the glucose predictions and their effects on decisions  
 to avoid hypo- and hyperglycemic events, the continuous error  
 grid analysis [33] has been used. The estimates of point and  
 rate precision are combined in a single accuracy assessment for  
 each of the BG ranges: hypoglycemia, euglycemia, and hyper-  
 glycemia. To this end, the point error grid analysis (P-EGA)  
 and the rate error grid analysis (R-EGA) are combined in the  
 three clinically relevant regions of hypoglycemia, euglycemia,  
 and hyperglycemia. Clinically accurate glucose predictions are

TABLE II  
ERROR MATRIX COMBINING R-EGA AND P-EGA

		P-EGA										
		Hypoglycemia			Euglycemia			Hyperglycemia				
		A	D	E	A	B	C	A	B	C	D	E
R-EGA	A	69.61	13.26	0.00	75.35	4.99	0.02	38.00	4.80	0.00	0.00	0.00
	B	6.63	1.10	0.00	8.84	1.41	0.00	29.20	5.20	0.00	0.00	0.00
	uC	0.00	2.76	0.00	4.22	1.38	0.07	17.20	0.00	0.00	0.00	0.00
	IC	6.08	0.55	0.00	3.16	0.54	0.01	5.60	0.00	0.00	0.00	0.00
	uD	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
	ID	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
	uE	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
IE	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	
AR		76.24			90.61			77.20				
BE		6.08			9.29			22.80				
ER		17.68			0.00			0.00				

AR: Accurate readings, BE: Benign errors, ER: Erroneous errors.

424 considered to be within the zones A and B on both P-EGA and  
425 R-EGA. Clinically benign errors correspond to acceptable point  
426 accuracy (i.e., A or B P-EGA zones) and significant errors in  
427 rate accuracy (i.e., C, D, or E R-EGA zones), which are unlikely  
428 to lead to negative clinical consequences. Clinically significant  
429 errors are those that could lead to a negative clinical action and  
430 therapeutic consequences.

431 From both the RMSE (mean  $\pm$  standard deviation (SD): 15.67  
432  $\pm$  6.03) and CC (mean  $\pm$  SD: 0.78  $\pm$  0.16), it is obvious that  
433 the predicted glucose profile follows the original one. Moreover,  
434 the error matrix combining P-EGA and R-EGA, presented in  
435 Table II, shows that erroneous errors are observed in the range  
436 of hypoglycemia.

437 Although the proposed glucose–insulin metabolism model  
438 uses CMs for the simulation of sc insulin kinetics and glucose  
439 absorption from the gut, similarly with the UVa T1DM sim-  
440 ulator, it adopts a completely different approach based on the  
441 RNN to map plasma insulin to sc glucose. The latter consists of  
442 the most essential module of the model. The previously presented  
443 prediction accuracy assessment refers to primarily testing the  
444 RNN and its effective combination with the CMs. The predic-  
445 tive performance of the glucose–insulin metabolism model has  
446 been assessed in a previous study [25], and the superiority of the  
447 used RNN over a feedforward neural network (FNN) has been  
448 demonstrated [26], using real patient data.

#### 449 B. IAS Tuning

450 The IAS provides the estimated insulin infusion rates every  
451 5 min. Regarding the performance envelope, lower  $y^l$  and up-  
452 per  $y^u$  bounds were chosen to be constant and equal to 90 and  
453 140 mg/dl, respectively, corresponding to a rather narrow target  
454 range. Particularly, 90 mg/dl corresponds to the minimum BG  
455 level of optimal glucose control [21], while 140 mg/dl is the  
456 maximum 2-h postprandial BG level [8]. Moreover,  $LG$  and  
457  $HG$  were set to 70 and 180 mg/dl, respectively, since, in this  
458 paper, BG concentrations between 70 and 180 mg/dl are con-  
459 sidered to be within the target range for T1DM. The values of  
460 the weighting coefficients  $\Gamma_L, \Gamma_H$ , and  $\Gamma_e$  were chosen to be 10,

TABLE III  
IIAS TUNING

Weighting Coefficients				Prediction, minimum and control horizon		
$\Gamma_{uv}$	$\Gamma_L$	$\Gamma_H$	$\Gamma_e$	$P_w$	$N_1$	$N_c$
10	10	1	100	10	1	1
Limits of performance envelop (mg/dl)				Glucose target range (mg/dl)		Reference glucose (mg/dl)
$y^l$		$y^u$		$LG$	$HG$	$r$
90		140		70	180	110

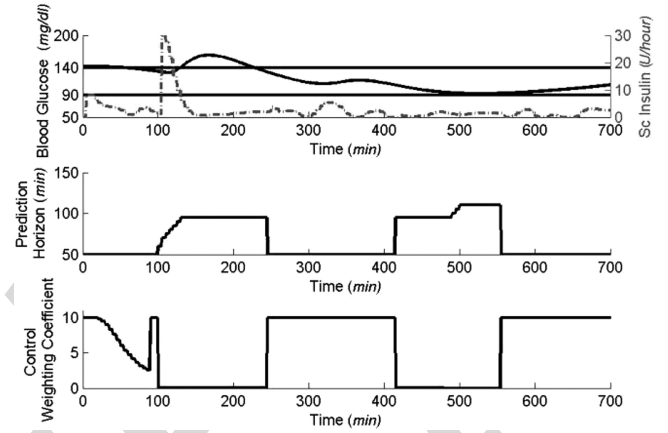


Fig. 4. Upper panel: Adult 5, sc insulin infusion rates (dashed-dotted line), BG data (solid line), limits of performance envelop [90–140 mg/dl] (dashed-line). Middle panel: Prediction horizon. Low panel: control weighting coefficient.

461 1, and 100, respectively. The rather large  $\Gamma_e$  value causes quite  
462 high insulin infusion rates, which are necessary to prevent hyper-  
463 glycemic episodes after meal ingestion. Furthermore,  $\Gamma_L$  is  
464 large enough to appropriately penalize for glucose predictions  
465 lower than 70 mg/dl and thus preventing from extremely high in-  
466 sulin infusion rates that would lead to hypoglycemic episodes.  
467 Parameter  $P_w$  is set to 10 corresponding to 50 min in order  
468 for the prediction horizon to account for sc insulin action. The  
469 control weighting coefficient  $\Gamma_{uv}$  is set to 10, which is high  
470 enough to ensure stability of the glucose controller.  $N_c$  is set to  
471 1 (its minimum possible value), corresponding to 5 min, in order  
472 to minimize on-line computation and  $N_1 = 1$  (see Section  
473 II-B). Moreover,  $u_{\min} = 0$ U/h while  $u_{\max} = 70$ U/h in accord-  
474 ance with the maximum allowable values for patients' safety  
475 and pump's hardware limitations [8]. The reference glucose  
476 level  $r$  is set to 110 mg/dl, which corresponds to the minimum  
477 value of the risk index. The numerical values of the parameters  
478 are summarized in Table III.

479 In order to clearly present the evolution of the prediction hori-  
480 zon  $N_p$  along with the control weighting coefficient  $\Gamma_u$  over  
481 time, the following simulation scenario has been studied: Adult  
482 5 was fed with 50 g at time 100 min. In Fig. 4, BG levels, sc  
483 insulin infusion rates along with prediction horizon, and control  
484 weighting coefficient are shown. As can be observed, the tuning  
485 algorithm does not always enter the triggered phase. It enters the  
486 triggered phase whenever there is danger for BG levels to ex-  
487 ceed the limits of the performance envelop (90–140 mg/dl), and

TABLE IV  
DAILY MEAL PROFILES

Day	1					2			
Meal Time (h)	07:00	12:00	16:00	18:00	23:00	07:30	13:00	18:30	
Meal Amounts (g)	45	70	0	5	80	5	40	85	60

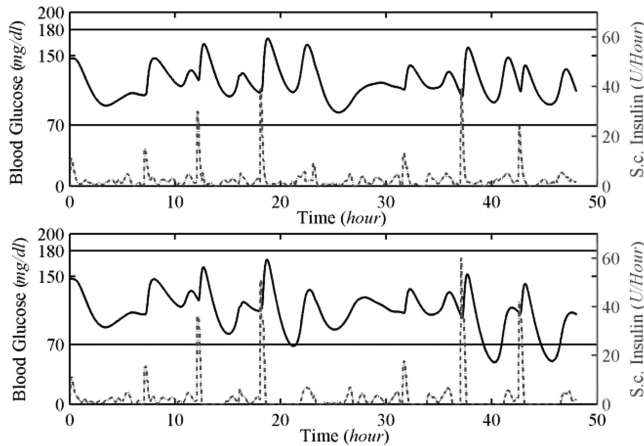


Fig. 5. Control results for Adult 3 under IIAS (upper panel) and fixed parameters NMPC (low panel). Estimated insulin infusion rates (dashed-dotted line), BG data (solid line), glucose target range [70–180 mg/dl].

488 appropriately updates the NMPC parameters, managing to reset  
489 and maintain glucose levels within the performance envelop.

### 490 C. Evaluation of the Controller—Simulation Scenarios

491 To evaluate IIAS’s performance under realistic conditions,  
492 several scenarios have been simulated. Particularly, the IIAS has  
493 been tested for its ability to handle meal disturbances, fasting  
494 conditions, interpatient variability, robustness against erroneous  
495 estimation of carbohydrates’ amount in ingested meals, and  
496 intraday variation in physiological parameters. Furthermore, in  
497 order to study the effectiveness of the tuning algorithm, two  
498 simulation scenarios have been studied: with (IIAS) and without  
499 (fixed parameter NMPC) the tuning algorithm.

500 1) *Evaluation of the IIAS Against Fixed Parameter NMPC:*  
501 Both controllers have been tested with the ten adults’ population.  
502 It should be noted that in the case of fixed parameter NMPC,  $N_p$   
503 and  $\Gamma_e$  are fixed over time and set both to 10. The simulation  
504 scenarios consider a two-day testing period with varying meal  
505 timings and amounts (see Table IV).

506 The superiority of the IIAS over fixed parameter NMPC is  
507 shown in Figs. 5 and 6. Fig. 5 presents the estimated sc insulin  
508 infusion rates along with the corresponding BG levels, when  
509 Adult 3 is fed with the two-day meal protocol and regulated  
510 using the IIAS (upper panel) and the fixed parameter NMPC  
511 (low panel), respectively. It should be noted that the controllers  
512 activate either the basal or the bolus action provided from the  
513 insulin pumps and hold the estimated insulin dose constant be-  
514 tween sampling instants (per 5 min). As shown in Fig. 5, the  
515 application of fixed parameter NMPC caused severe hypogly-  
516 caemic episodes, which are defined as BG levels lower than

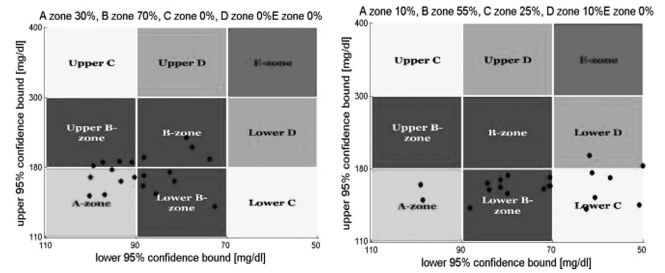


Fig. 6. CVGA for the ten adults of the Uva T1DM simulator. *left*: IIAS (30% in zone A and 70% in zone B). *Right*: NMPC (10% in zone A, 55% in zone B, 25% in zone C, and 10% in zone D).

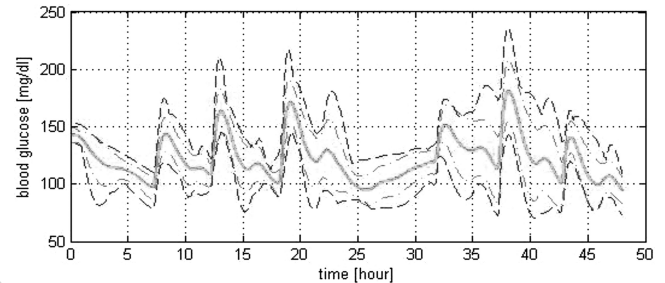


Fig. 7. BG trace for the ten adults of the Uva T1DM simulator when the IIAS is applied. Mean response (solid curve), SD (dashed-dotted curve), and min/max envelop (dashed curve).

60 mg/dl [9]. On the other hand, the IIAS managed to main- 517  
518 tain BG levels within the target range (70 --180 mg/dl), while  
519 achieving less fluctuations over time.

520 The control variability grid analysis (CVGA) [34], shown in  
521 Fig. 6, serves as a tool to evaluate the controllers with the en-  
522 tire population. Each point in the CVGA represents the lower and  
523 the upper bound of 95% confidence interval of BG data for  
524 one patient during one day. Zones A and B are considered to  
525 represent good glucose control. CVGA demonstrates that IIAS  
526 provides superior performance over the fixed parameter NMPC,  
527 managing to keep all the patients inside the zones A and B.  
528 Furthermore, the min/max envelop presented in Fig. 7 indicates  
529 that the BG levels for the hard-to-control patients are within  
530 the acceptable range 70–236 mg/dl, managing to avoid hypo-  
531 glycemic episodes and severe hyperglycemic episodes (above  
532 280 mg/dl).

533 Moreover, numerical metrics of average glycemia, percentage  
534 within the target range (70–180 mg/dl), risk associated with ex-  
535 treme glucose deviations [35] (low blood glucose index (LBGI),  
536 high blood glucose index (HBGI), and total risk index), are used  
537 to provide more details about the controller performance. In Ta-  
538 ble V, the obtained numerical results, when the IIAS is applied  
539 on all 10 patients, are presented. It can be seen that most of the  
540 time, BG levels are kept within the target range, while the risk  
541 indices (LBGI, HBGI, and total risk index) have low values,  
542 showing that tight glycemic control is achieved.

543 2) *Robustness to Meal Estimation Errors:* Since the pro-  
544 posed IIAS is informed about the carbohydrates amount of the  
545 upcoming meal, its ability to handle meal estimation errors is  
546 of utmost importance. To this end, the IIAS has been tested

TABLE V  
CONTROL PERFORMANCE OF THE IIAS AND THE OPEN-LOOP PREADJUSTED TREATMENT

Simulation scenario	mean BG Mean ( $\pm$ SD)	Pre meal BG Mean ( $\pm$ SD)	Post meal BG Mean ( $\pm$ SD)	% below target Mean ( $\pm$ SD)	% above target Mean ( $\pm$ SD)	% within target Mean ( $\pm$ SD)	LBGI Mean ( $\pm$ SD)	HBGI Mean ( $\pm$ SD)	risk index Mean ( $\pm$ SD)
Accurate meal announcement (IIAS)	122.25 (9.06)	114.27 (12.31)	139.78 (9.19)	0 (0)	2.51 (2.76)	97.49 (2.76)	0.35 (0.35)	1.09 (0.64)	1.45 (0.66)
40% OEE (IIAS)	117.54 (7.91)	105.57 (8.99)	132.26 (12.68)	1.01 (1.51)	2.40 (3.13)	96.58 (2.83)	0.72 (0.34)	0.92 (0.62)	1.64 (0.66)
40% UEE (IIAS)	120.28 (10.61)	110.11 (11.13)	137.44 (14.30)	5.15 (5.07)	4.36 (4.43)	90.48 (6.66)	0.99 (0.71)	1.27 (0.86)	2.26 (1.10)
Intraday variation in physiological parameters (IIAS)	122.47 (7.58)	128.25 (15.79)	133.31 (15.42)	0.66 (0.87)	3.41 (3.25)	95.91 (3.61)	0.4 (0.27)	1.2 (0.65)	1.6 (0.71)
Open loop preadjusted treatment	130.50 (6.92)	124.4 (6.65)	145.16 (10.80)	1.14 (3.61)	3.68 (3.78)	95.17 (5.59)	0.30 (0.48)	1.65 (0.69)	1.96 (0.91)

547 against overestimation errors (OEE) and underestimation errors  
548 (UEE) up to 40%. Table V demonstrates the mean values and the  
549 SDs of the numerical metrics over the results obtained for the  
550 ten adults. Although certain hypoglycemic and hyperglycemic  
551 episodes occurred, none of them was severe. It is noteworthy  
552 that the IIAS is able to handle meal estimation errors and regu-  
553 late properly insulin infusion rate, in order to keep glucose  
554 within the target range most of the time.

555 3) *Robustness Against Intraday Variation in Physiological*  
556 *Parameters:* One of the critical challenges for a glucose con-  
557 trol algorithm is robustness against intraday variation in phys-  
558 iological parameters. In order to represent diurnal metabolic  
559 variations, time variation of the *in silico* patient-specific phys-  
560 iological parameters was considered, as drawn from a normal  
561 distribution with SD of 10%. This distribution was chosen to  
562 capture the expected variation in insulin sensitivity [36]. In Table  
563 V, the obtained numerical results over the ten adults are  
564 presented. The IIAS achieved good glucose control, managing  
565 to maintain BG levels within the acceptable range for 95.17%  
566 of the total time, avoiding severe hypoglycemic and hyper-  
567 glycemic episodes. Furthermore, the risk indices are low, prov-  
568 ing the IIAS' ability to handle intraday variation in physiological  
569 parameters.

#### 570 D. Comparison of the IIAS With Other Glucose Controllers

571 In order to prove the efficacy of the IIAS, its performance has  
572 been compared with that of other open-loop and closed-loop  
573 glucose controllers.

574 1) *Open-Loop Preadjusted Treatment:* The open-loop  
575 preadjusted treatment is supported by the UVa T1DM simulator.  
576 The ten *in silico* adults of the simulator followed a protocol of  
577 meals presented in Table IV. A matching insulin bolus and a  
578 basal rate were provided by the UVa T1DM simulator for each  
579 *in silico* adult and the results obtained by applying the open-  
580 loop preadjusted treatment are presented in Table V. It can be  
581 observed that the IIAS achieves better glucose control.

582 2) *Adaptive Basal Therapy:* Since the basal rate provided  
583 by the UVa T1DM simulator is nonoptimal, the IIAS has been  
584 compared with adaptive basal therapy [37]. The latter suggests  
585 adaptation of the basal rate as a gain multiplier based on the cur-

TABLE VI  
COMPARISON OF THE IIAS WITH THE ADAPTIVE BASAL THERAPY [37]

Controller	Hypo- percent (<60mg/dl)	Hyper- percent	Safe percent	risk index
IIAS	0.00 $\pm$ 0.00	0.60 $\pm$ 1.52	99.40 $\pm$ 1.52	0.99 $\pm$ 0.43
Adaptive Basal Therapy	0.5 $\pm$ 0.01	1.3 $\pm$ 0.03	98.2 $\pm$ 0.03	1.7 $\pm$ 0.59

586 rent CGM glucose value and its rate of change. Identical meals  
587 used in [37] provided input to the ten *in silico* adults, which were  
588 regulated by the IIAS. In particular, the ten *in silico* adults fol-  
589 lowed a one-day meal scenario of 40, 75, 60 g of carbohydrates  
590 at 7:00 A.M., 12:00 A.M., and 6:00 P.M., respectively. Results ob-  
591 tained from the application of the IIAS and the adaptive basal  
592 therapy are presented in Table VI in terms of hyperglycemia  
593 and severe hypoglycemia (<60 mg/dl) along with risk indices.  
594 It can be observed that the IIAS provides better glucose control  
595 performance.

596 3) *Artificial Pancreatic  $\beta$ -Cell Based on Zone-MPC:* In order  
597 to justify the use of the proposed nonlinear approach to  
598 improve glucose control, the IIAS has been compared with an ar-  
599 tificial pancreatic  $\beta$ -cell based on zone-MPC that uses mapped-  
600 input data and is adjusted automatically by linear difference  
601 personalized models [38]. The ten *in silico* adults followed the  
602 three meal scenario used in [38]—consisting of 75, 75, and 50 g  
603 of carbohydrates at 7 A.M., 1 P.M., and 8 P.M., respectively—and  
604 were regulated by the IIAS. The obtained results are presented  
605 in Table VII. It should be noted that no severe hypoglycemic  
606 (<60 mg/dl) and hyperglycemic episodes (>280 mg/dl) have  
607 been observed during the operation of the IIAS- and zone-MPC-  
608 based glucose controllers. As discussed in [38], a single severe  
609 hypoglycemic event occurred during the operation of the MPC  
610 with set point at 110 mg/dl. When the *in silico* adults were regu-  
611 lated by the IIAS, the mean glucose value was closer to the  
612 desired glucose level, while the average SD of the mean glucose  
613 value was lower, indicating lower variability in glucose con-  
614 trol performance among the *in silico* adults. Furthermore, lower

TABLE VII  
COMPARISON OF THE IIAS WITH THE ARTIFICIAL PANCREATIC B-CELL [38]

Controller	Mean Glucose	Hyper- percent
IIAS	117.61 ± 7.11	0.81 ± 2.05
Zone-MPC (bounds: 80-140 mg/dl) (Experiment 5 in [38])	152.00 ± 28.00	27.99 ± 20.51
Zone-MPC (bounds: 100-120 mg/dl) (Experiment 6 in [38])	141.00 ± 29.00	20.75 ± 19.45
MPC (set-point 110 mg/dl) (Experiment 7 in [38])	136.00 ± 29.00	17.54 ± 18.58

percentage of hyperglycemia was observed during the operation of the IIAS. The obtained improved glucose control performance is related to higher on-line computation.

Summarizing, the use of a data-driven model for the simulation of the blood glucose–insulin kinetics (real-time self-adaptive NN) permits personalization of the system and efficient handling of a changing environment. It is important to note that the incorporation of the RNN makes the model capable of simulating glucose–insulin kinetics taking into account patient specific information related to ingested carbohydrates, sc insulin infusion rate, and glucose records from CGMS that are usually available in clinical practice. The metabolic behavior of a specific patient is captured through the real-time update of the RNN’s weights. Whenever a new glucose measurement is applied to the model, the RNN’s weights are appropriately adapted in order to adjust to the new metabolic behavior. According to above, the RNN consists the most essential module of the personalized glucose–insulin metabolism model. Thus, the similarities of the latter with the UVa T1DM simulator regarding the use of CMs for the sc insulin kinetics and the glucose absorption from the gut do not limit the reliability of the presented assessment of the IIAS performance. This is of particular importance since the IIAS has demonstrated robustness against intraday variation in physiological parameters. Moreover, the tuning algorithm for the real-time update of the NMPC control parameters greatly improved controller’s performance, demonstrating its importance toward the tuning of glucose controllers based on MPC.

Clinical evaluation of the IIAS on real T1DM patients is in progress. Future research activities are focused on the optimization of the proposed IIAS and its complete integration into a telecommunication platform for the efficient management and treatment of patients with T1DM [39].

#### IV. CONCLUSION

A novel IIAS based on NMPC has been proposed in order to estimate optimal insulin infusion rates. The proposed approach introduces 1) a personalized model based on the combined use of CMs and an RNN for the simulation of glucose–insulin metabolism and 2) an automatic algorithm for the on-line adaptation of NMPC parameters. The performance of the IIAS has been *in silico* evaluated using the ten adults’ population, available in the training version of the UVa T1DM simulator. The obtained results demonstrate that the proposed IIAS is robust

with respect to its ability to handle various conditions characterized by sensor errors, lags, meal disturbances, large meal estimation errors, interpatient variability, and intraday variation in physiological parameters.

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She is the author or coauthor of 141 papers in refereed international journals and chapters in books, and more than 250 papers in international conference proceedings. She is author or coauthor of two books in Greek and the co-editor of one book in English published by Springer. She holds two patents. She has been the Technical Manager of several European and National Research and Development projects in the field of biomedical engineering. She has been honorary chair/ chair/member of the program/organizing committee of more than 50 international conferences on the same fields. She has served as keynote/invited speaker at several international conferences, symposia and workshops organized by NATO, WHO, ICNIRP, IEEE, URSI, COMCON, PIERS, etc. She has been the advisor of 17 completed Ph.D. theses, several of which have received various awards. She has served as external evaluator in numerous University promotion committees and in international and national committees for grant proposal applications. Her current research interests include biomedical signal and image processing and analysis, biomedical informatics, simulation of physiological systems, medical imaging, and biological effects and medical applications of radio frequency electromagnetic fields.

Dr. Nikita is a member of the Editorial Board of the TRANSACTIONS ON BIOMEDICAL ENGINEERING and a Guest Editor of several international journals on biomedical engineering subjects. She received various honors/awards, among which, the prestigious Bodossakis Foundation Academic Prize for exceptional achievements in “Theory and Applications of Information Technology in Medicine” (2003). She is a member of the Board of Directors of the Hellenic National Academic Recognition and Information Center and a member of the National Council of Research and Technology. She is a member of the Technical Chamber of Greece and the Athens Medical Association. She is also the Founding Chair and Ambassador of the Engineering in Medicine and Biology Society, Greece chapter, Vice Chair of the IEEE Greece Section, and the Deputy Head of the School of Electrical and Computer Engineering, NTUA.

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